

Integrating Vehicle Routing and Motion Planning

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1. New problem: Waypoint Allocation and Motion Planning
 - (a) WAMP combines task planning and motion planning
 - (b) vehicle routing but now with *real* routing!
2. Efficient solver
 - (a) integrates tabu search, blind search, heuristic search, linear programming and simple temporal networks
3. Meets application requirements
 - (a) 2.5x faster and more scalable than industrial partner's

Combining Vehicle Routing and Motion Planning

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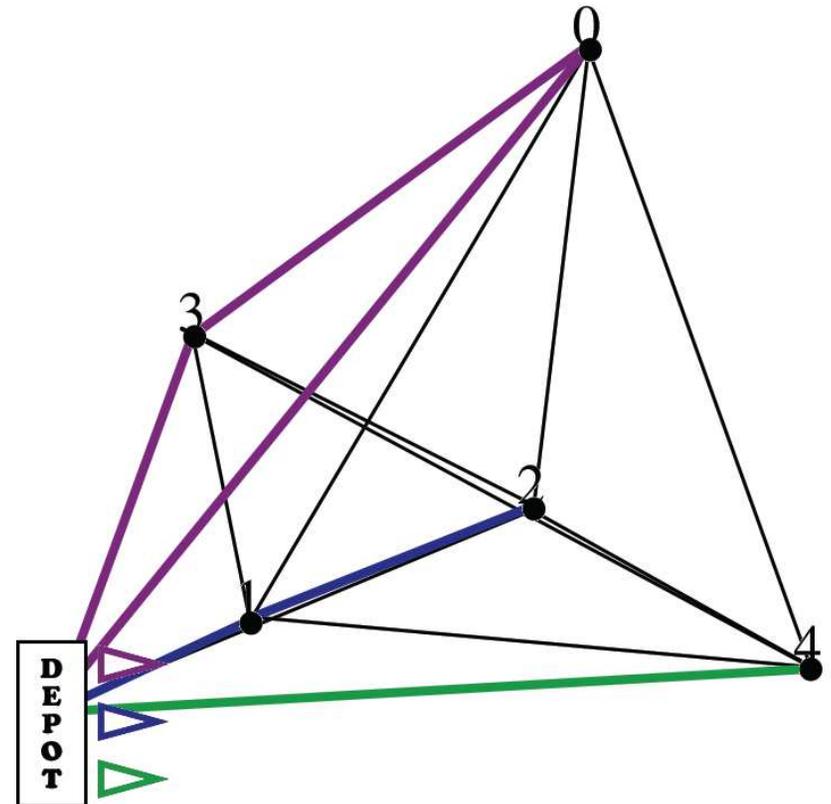
Vehicle Routing

allocate tasks to vehicles

routes given as a distance matrix

objective: find cheapest ordering

temporal constraints



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Motion Planning

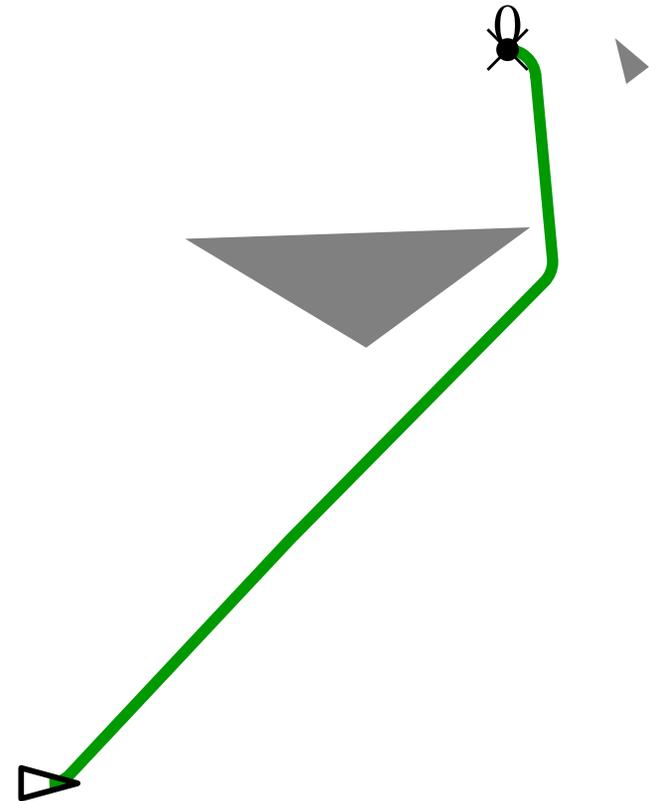
find feasible trajectory

continuous space

respect vehicle limitations

obstacles

objective: minimize time



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WAMP

allocate tasks to vehicles

~~routes given as a distance matrix~~

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temporal constraints

find feasible trajectory

continuous space

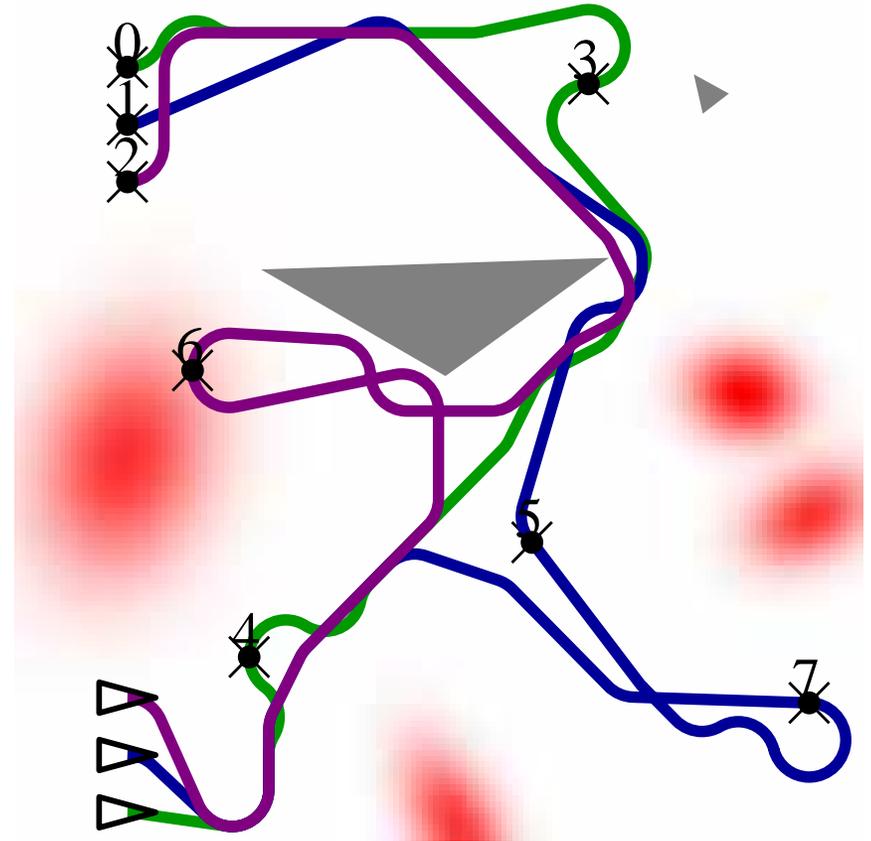
respect vehicle limitations

obstacles

~~objective: minimize time~~

varying traversal costs

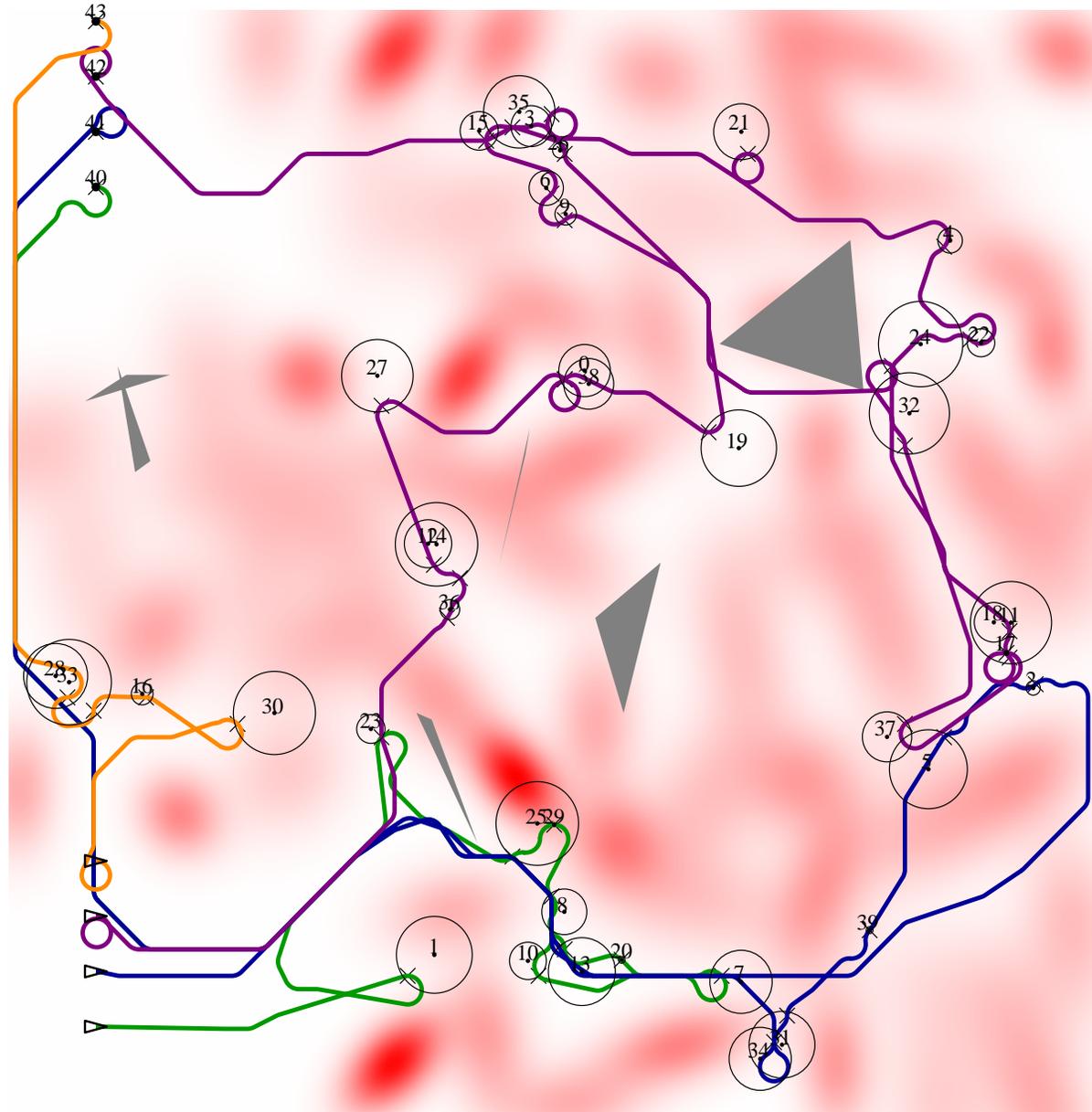
objective: minimize time and cost



naturally combines task allocation and motion planning

A Realistic-Sized Instance

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Application: Battlespace Management

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A large instance:

- 16 aircraft
 - varying velocities and turning radii
- 40 waypoints
 - time windows
 - relative temporal constraints
- 40 radar sensitive (cost) zones
- strict no-fly zones
- 7 second time limit

Central Challenge

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1. Can't do task allocation without routing costs
need cost from one waypoint to next
2. Can't find routing costs without motion paths
paths may intersect areas of high cost
3. Can't find motion paths without leg durations
is there time to navigate around high cost?
4. Can't assign leg durations without **time/cost tradeoff**
which legs benefit most from additional time?

Surrogate Objective

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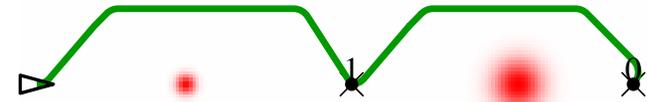
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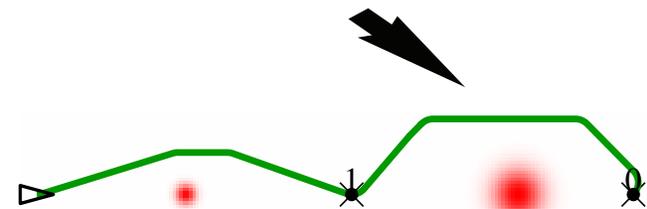
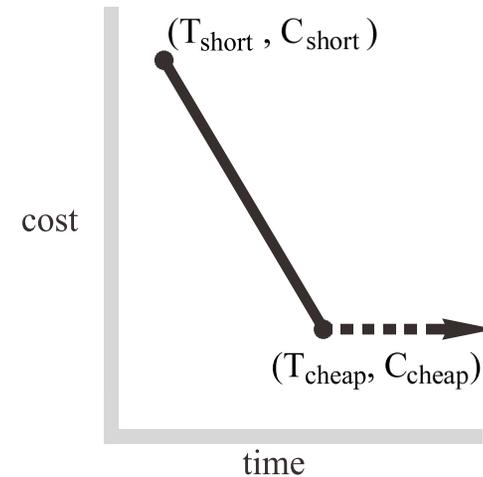
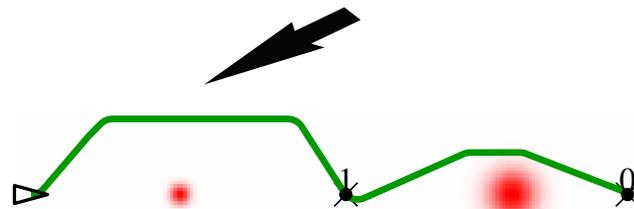
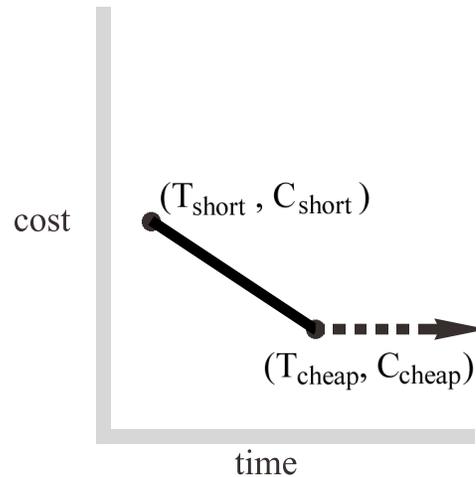
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fastest route is too expensive



cheapest route is too long



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1. Precomputation: find surrogate objective endpoints



surrogate objective

2. Sequencer: assign and order waypoints to vehicles



ordering

3. Linear Program: assign timepoints to waypoints



timetable

4. Routing: find motion plans between waypoints

5. (Feedback: provide new information to previous layers)



new constraints

Step 1: Precomputation

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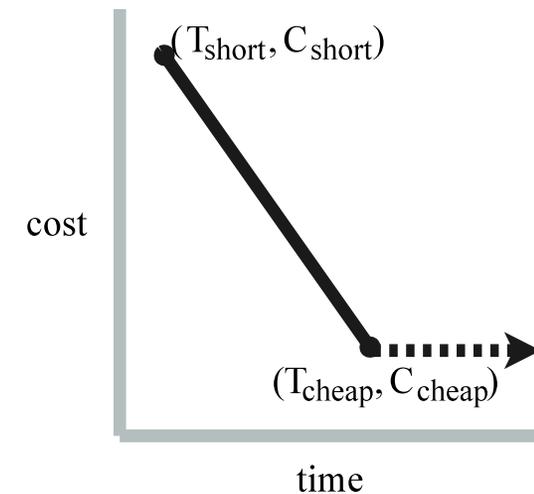
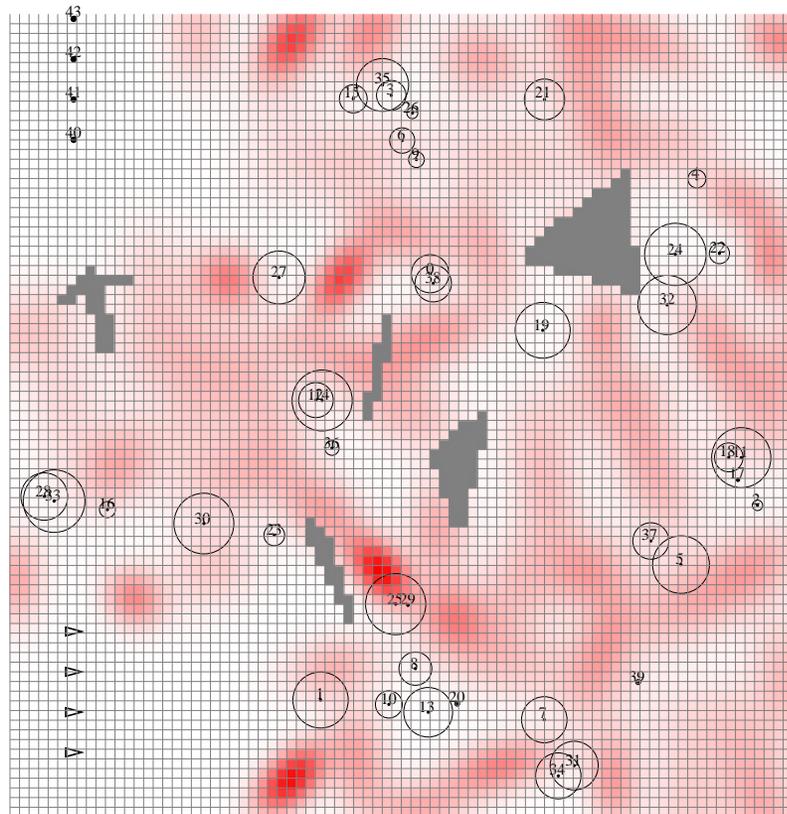
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Input: problem

Output: surrogate objective

Techniques: Dijkstra



Step 2: Sequencer

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Input: surrogate objective

Output: feasible ordering : $\{w_2, w_3, w_1\}$

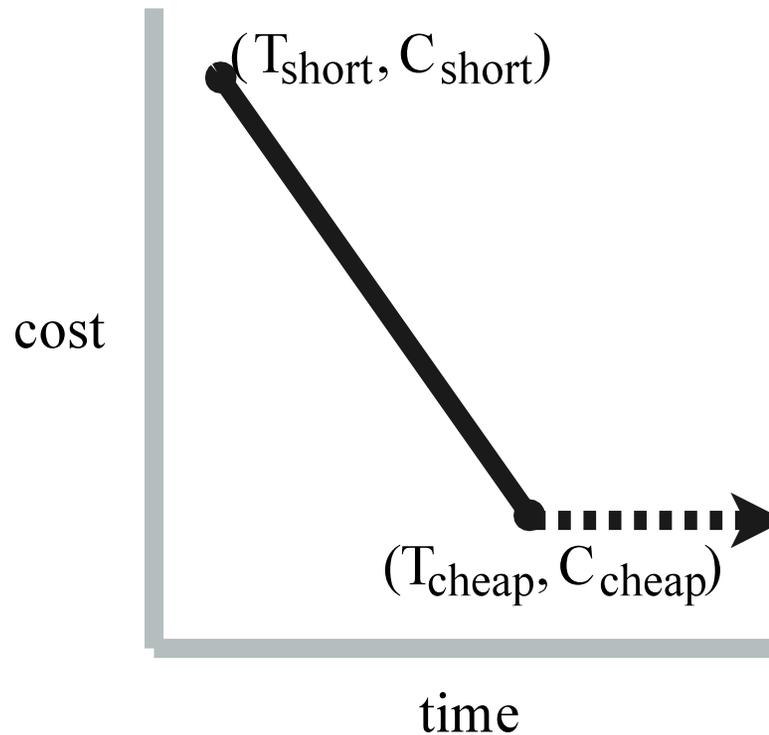
Techniques: tabu search (based on *Lau, Sim and Teo, 2003*)
simple temporal network (STN)

Step 3: Linear Program

Input: feasible ordering : $\{w_2, w_3, w_1\}$, surrogate objective

Output: timetable : $\{w_2 = 2, w_3 = 3, w_1 = 5\}$

Techniques: linear programming



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Step 4: Router

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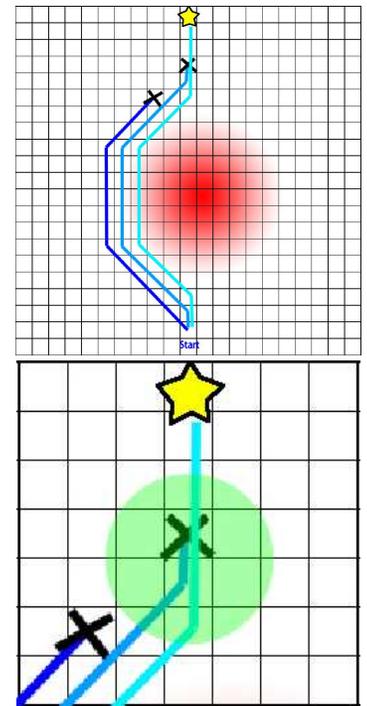
Conclusion

Input: timetable : $\{w_2 = 2, w_3 = 3, w_1 = 5\}$

Output: solution

Techniques: discretized A^* search $\langle location, time \rangle$, smoothing

- discretized A^* search
- temporal pruning: $t(s, n) + \hat{t}(n, g) > TT(g)$
- re-expansions: $g(n) < g(n')$ but $t(n) > t(n')$
- resumable



Step 4: Router

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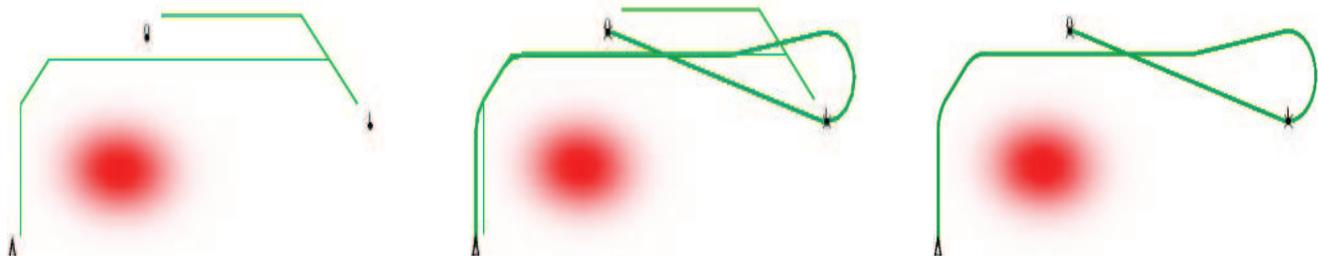
Conclusion

Input: timetable : $\{w_2 = 2, w_3 = 3, w_1 = 5\}$

Output: solution

Techniques: discretized A* search $\langle location, time \rangle$, smoothing

■ smoothing



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Router : leg can not be routed to achieve timetable



new constraints

Linear Program : LP can not be solved with new constraint



new constraints

■ Sequencer

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Experiment: Small Instance Scaling

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■ **Small Instances**

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Test scalability against a unified A* Search
single vehicle $\langle x, y, \theta, t \rangle$
no temporal constraints
spanning tree heuristic
infinite time w/bounded memory (7.5GB)

# Waypoints	Failure Rate
1	24%
2	64%
3	88%
4	98%
5	98%
6	100%

Generic A* does not scale to meet our requirements

Experiment: Sequencer Stressing

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■ Small Instances

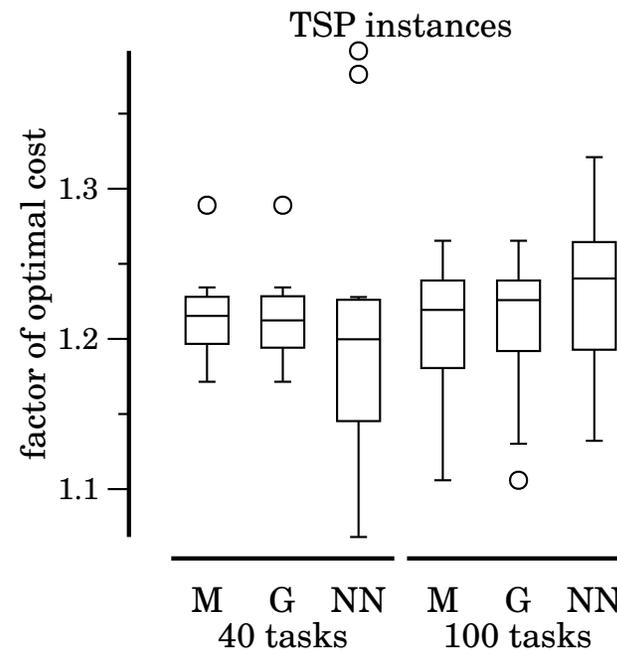
■ Sequencer

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Test ability to find quality orderings
single vehicle with ϵ turn radius
no temporal constraints
uniform cost and no keep-out zones



The sequencer produces near optimal waypoint orderings for
TSP instances

Experiment: Realistic Instances

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■ Small Instances

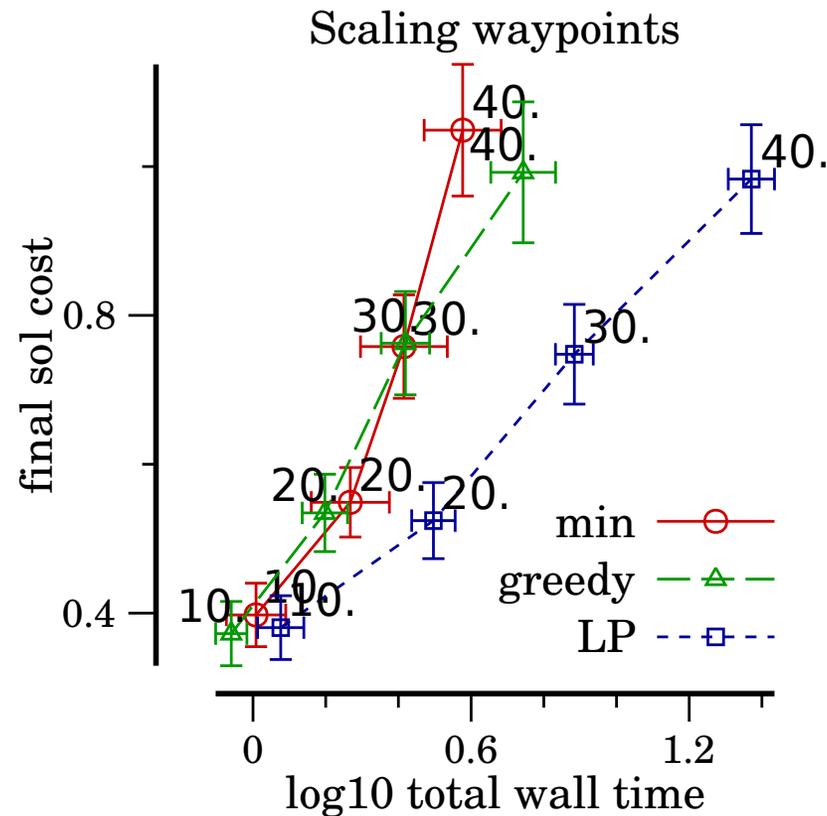
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Test effects of scaling the number of waypoints
4 vehicles



The system scales with an increasing number of waypoints

Experiment: Realistic Instances

Test effects of scaling the number of vehicles
20 waypoints

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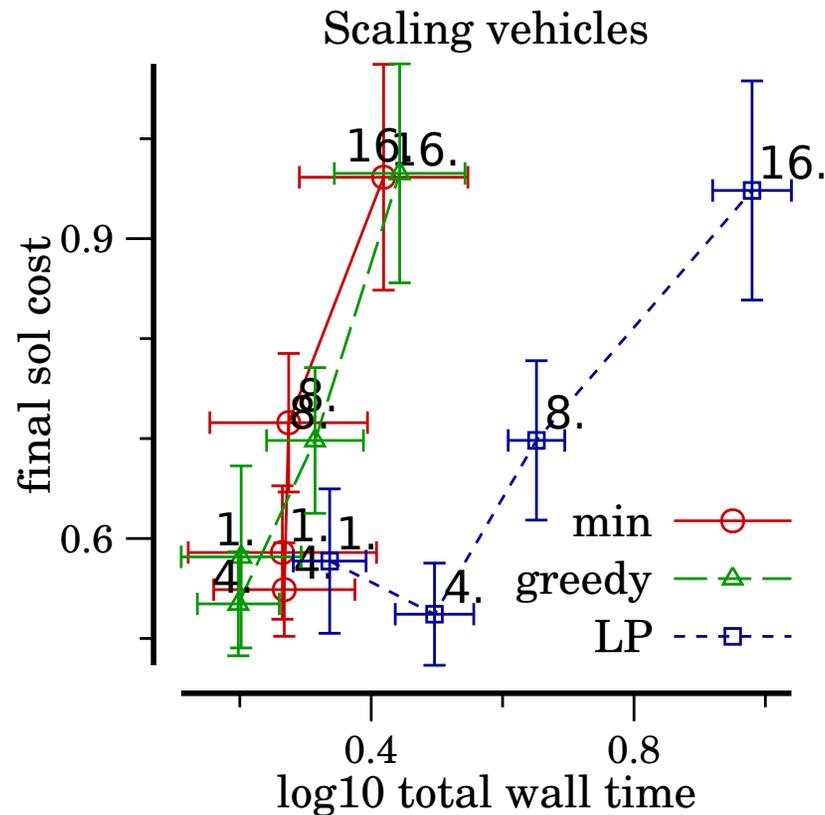
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The system scales with an increasing number of vehicles

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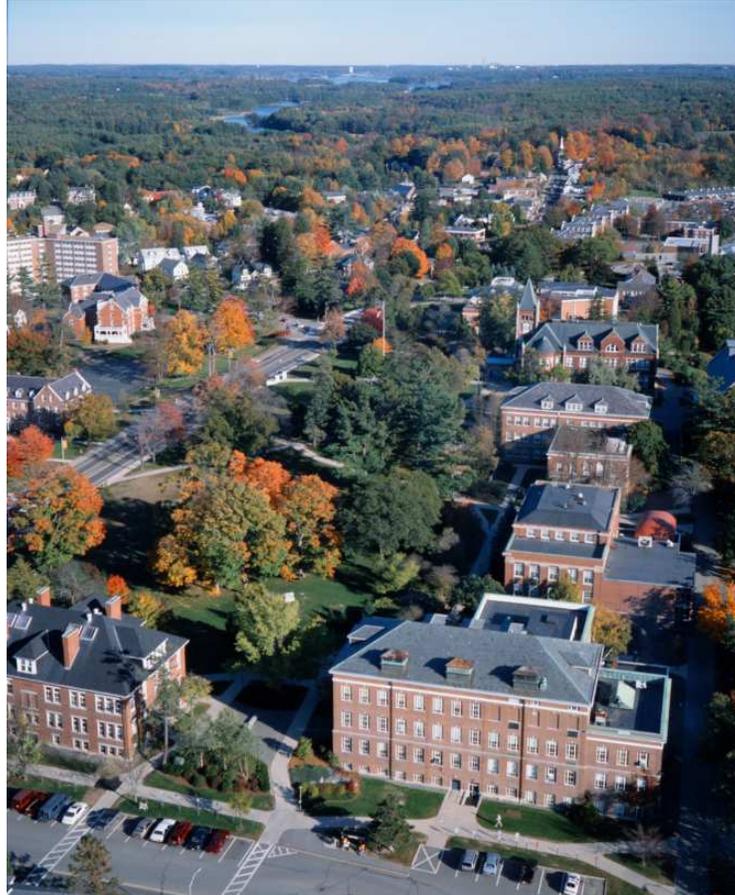
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- friendly faculty
- funding
- individual attention
- beautiful campus
- low cost of living
- easy access to Boston, White Mountains
- strong in AI, infoviz, networking, bioinformatics

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■ Formulation

Back-up Slides

Problem Formulation

WAMP : $\langle Size, V, W, K, C, R \rangle$

- V : Vehicles

$$v_i = \langle x_0, y_0, \theta_0, v, r \rangle$$



- W : Waypoints

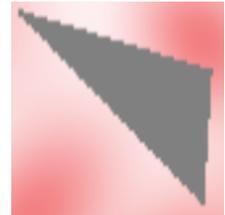
$$w_i = \langle x, y, r, \theta_0, \theta_1, t_s, t_e, A \rangle$$

$$A \subseteq V$$



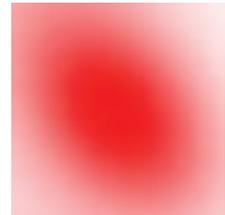
- K : Keep-Out Zones

$$k_i = \langle x_0, y_0, x_1, y_1, x_2, y_2 \rangle$$



- C : Cost Zones

$$c_i = \langle x, y, h, \sigma_x, \sigma_y, c \rangle$$



- R : Relative Constraints

$$r_i = \langle w_i, w_j, min, max \rangle$$

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