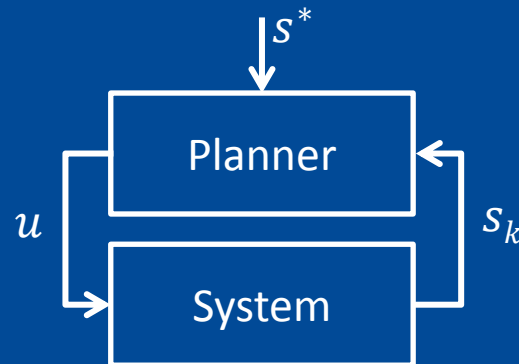


A Planning Based Framework for Controlling Hybrid Systems



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Outline



Motivation

From Continuous
Dynamics...

... to a
Domain Model

Domain Predictive Control

Exemplary Simulation

Discussion

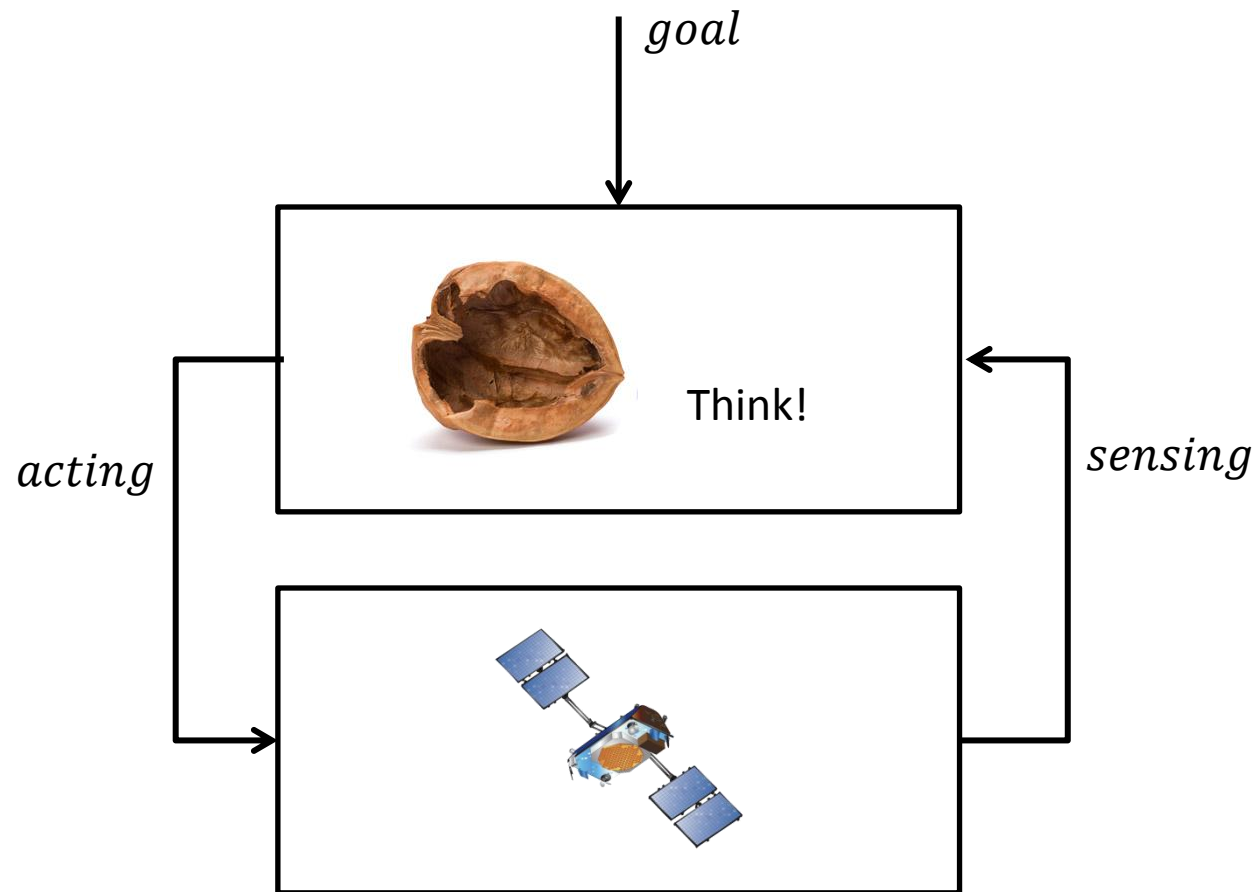
Outlook

Motivation



Lunar Lander ExoMars

Motivation





- **Key Aspects**

- Hybrid Systems**

- Continuous Dynamics

- Boolean State Variables

- Autonomy**

- Reduction of Computational Effort

- Quick Decision Generation

- Exogenous Events**

- Obstacles

- Reactivity

Outline



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From a Hybrid System...



Hybrid System

$$\dot{\mathbf{x}}_n(t) = A(\mathbf{x}_l) \mathbf{x}_n(t) + B(\mathbf{x}_l) \mathbf{u}(t)$$

Planning Task

Find $\mathbf{u}(t)$, $t \in [t_a, t_b]$ such that:

$$\begin{array}{ccc} \mathbf{x}_n(t_a) & \longrightarrow & \mathbf{x}_n(t_b) \\ \text{Initial State} & & \text{Desired State} \end{array}$$

...to a Planning Action...



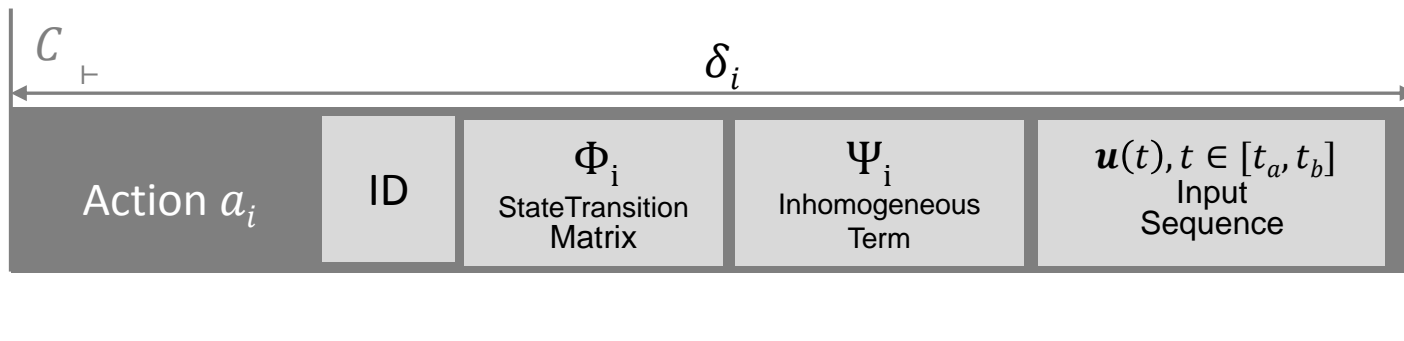
1. Anticipate some input fragments
 $\mathbf{u}_i(t), t \in [0, \delta_i]$

2. Solve the differential equations
(preprocessing step)

$$\Phi = e^{A(x_l) \delta_i}$$

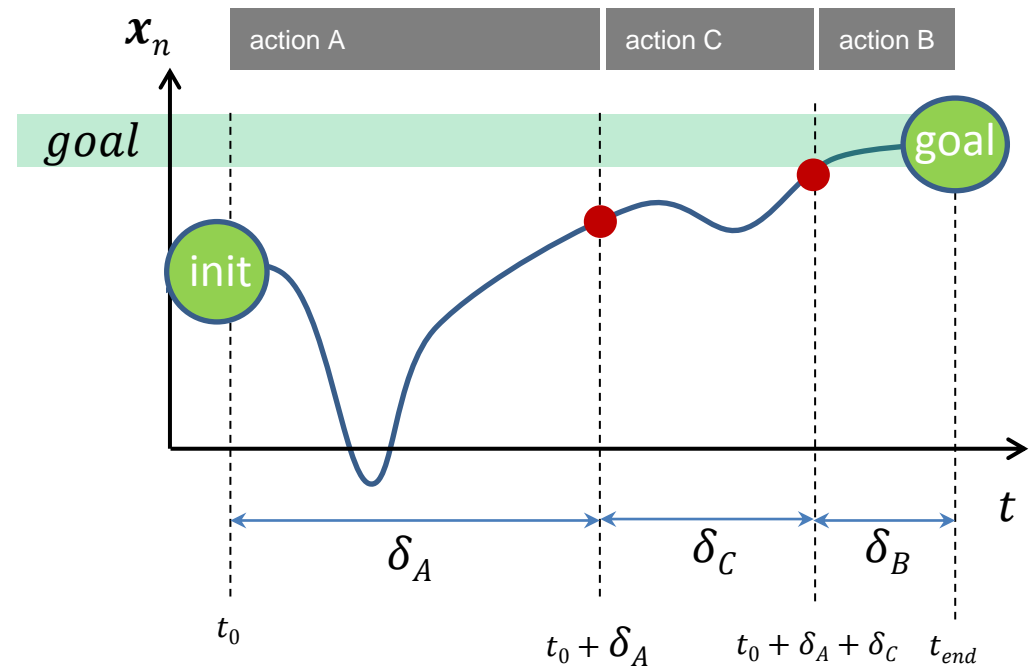
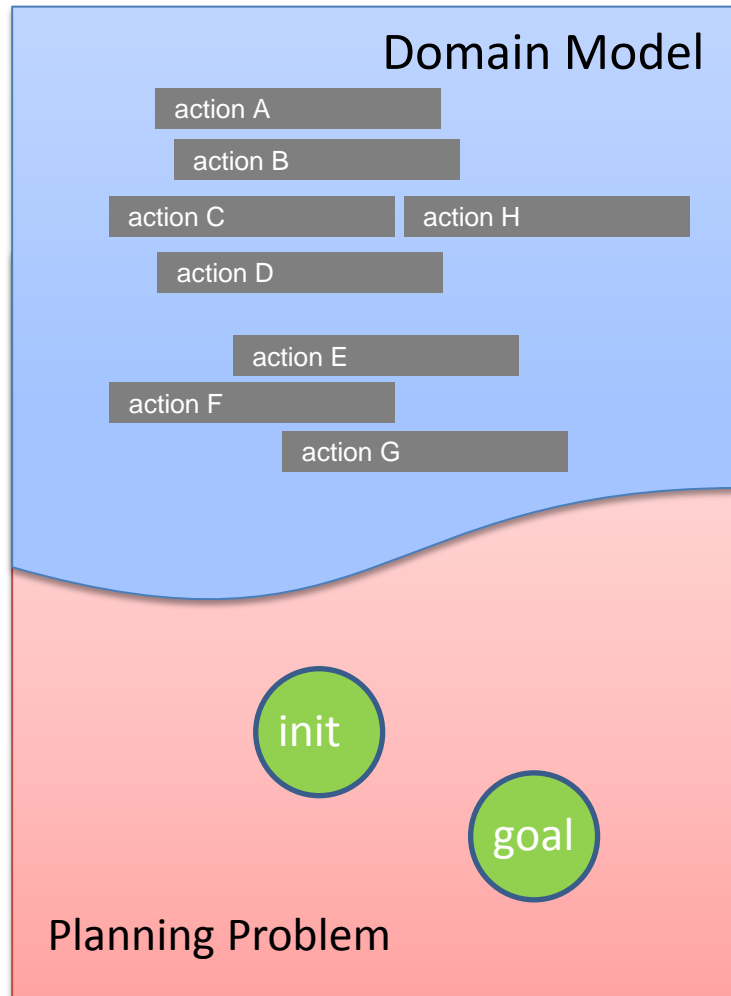
$$\Psi = \int_{t_0}^{t_0 + \delta_i} e^{A(x_l) \cdot (t_0 + \delta_i - \tau)} B(x_l) \mathbf{u}(\tau) d\tau$$

3. Generate planning action



$$E_{-} : \quad \mathbf{x}_n(t_0 + \delta_i) = \Phi_i \mathbf{x}_n(t_0) + \Psi_i$$

... to the Domain Model



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Remember the Key Aspects



- Key Aspects

Hybrid Systems

Continuous Dynamics

Boolean State Variables

Autonomy

Reduction of Computational Effort

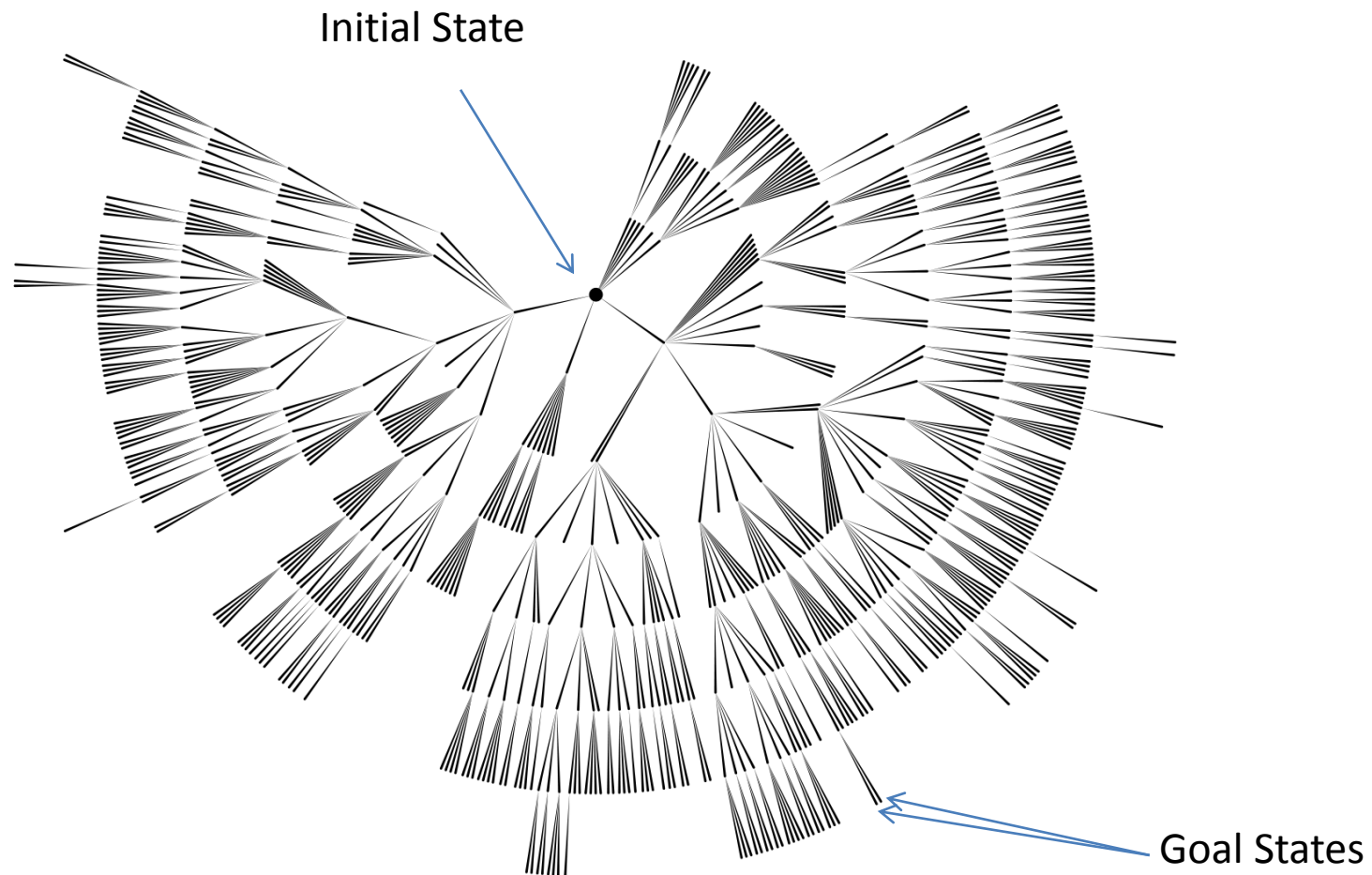
Quick Decision Generation

Exogenous Events

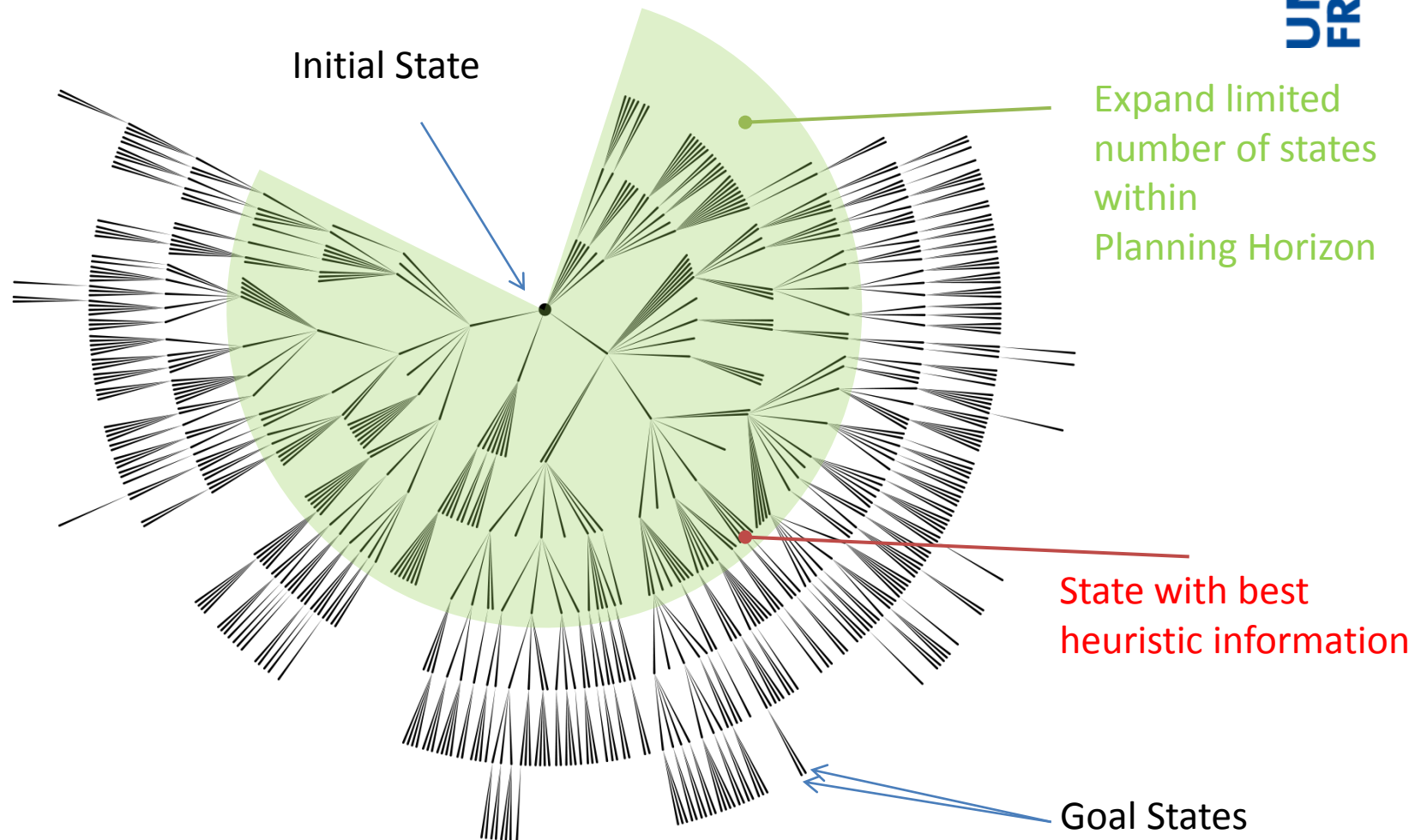
Obstacles

Reactivity

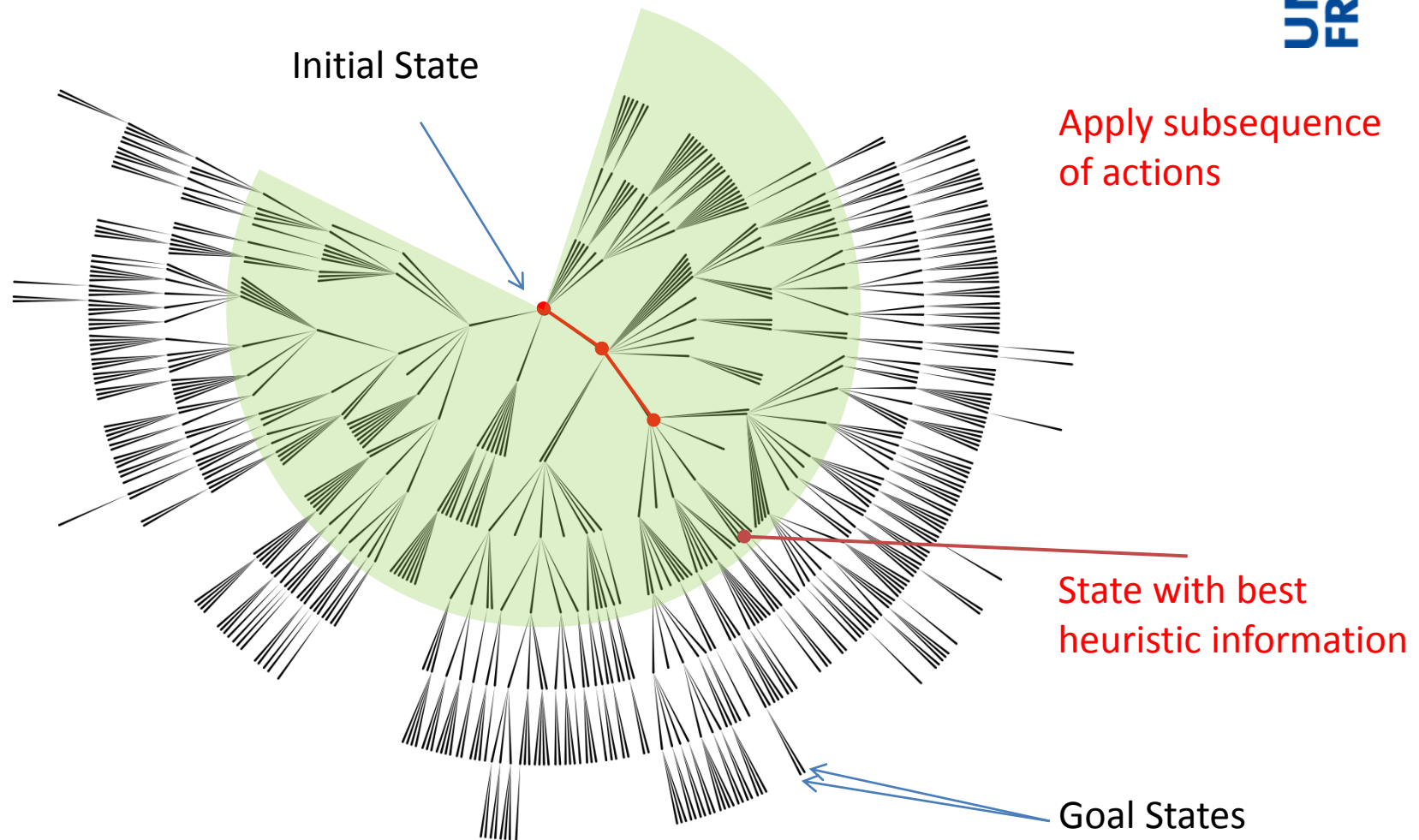
Domain Predictive Control



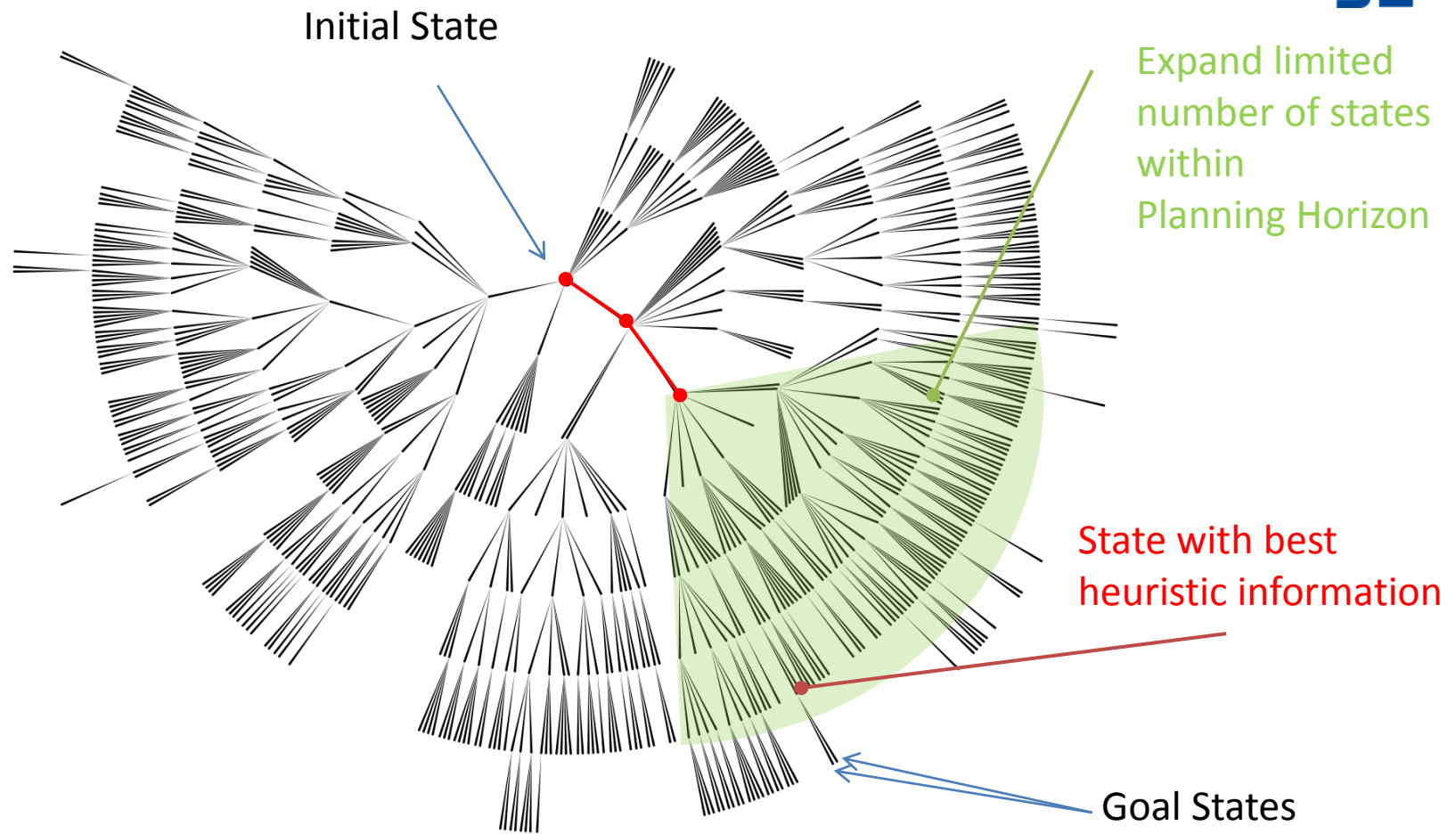
Domain Predictive Control



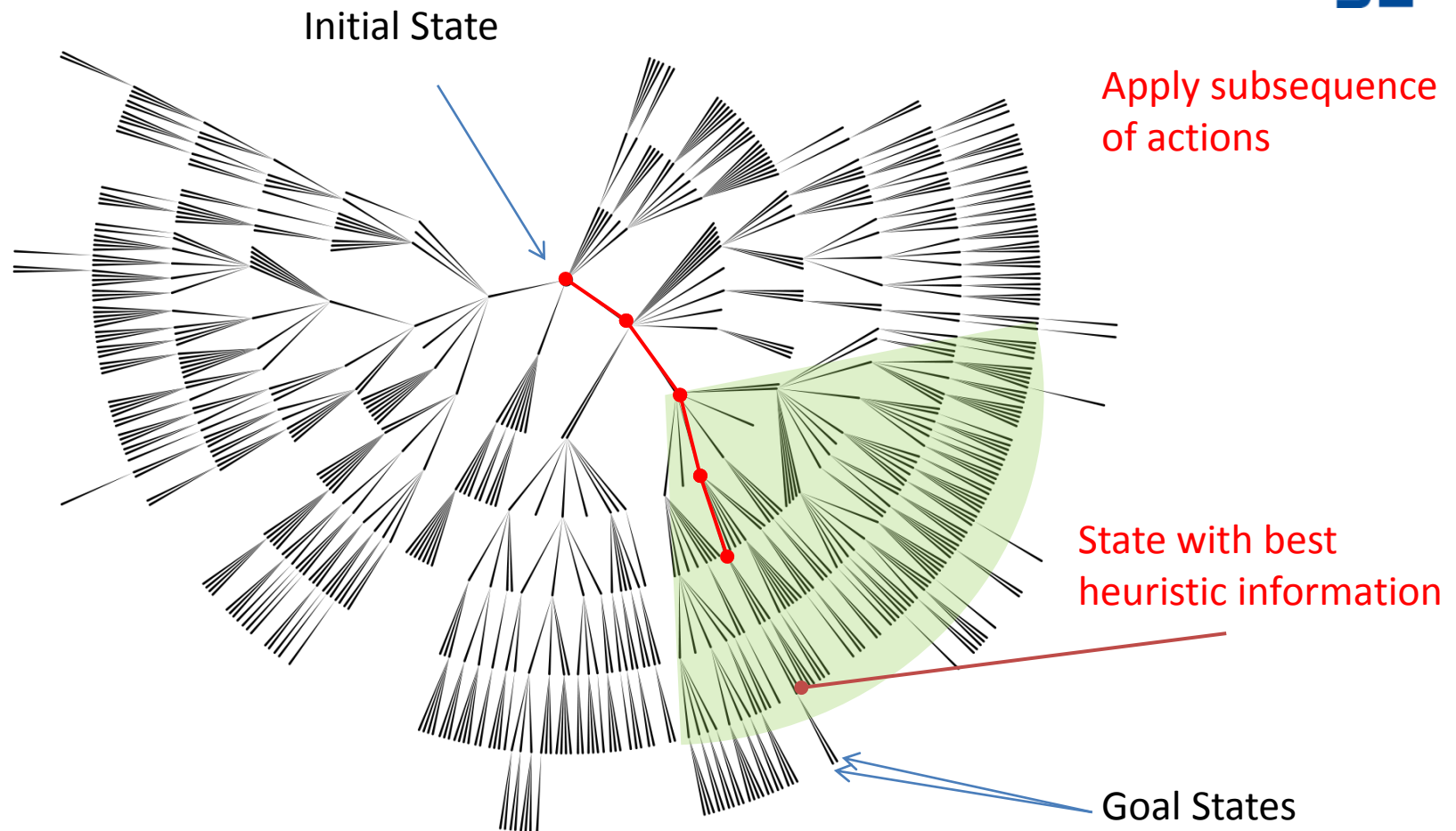
Domain Predictive Control



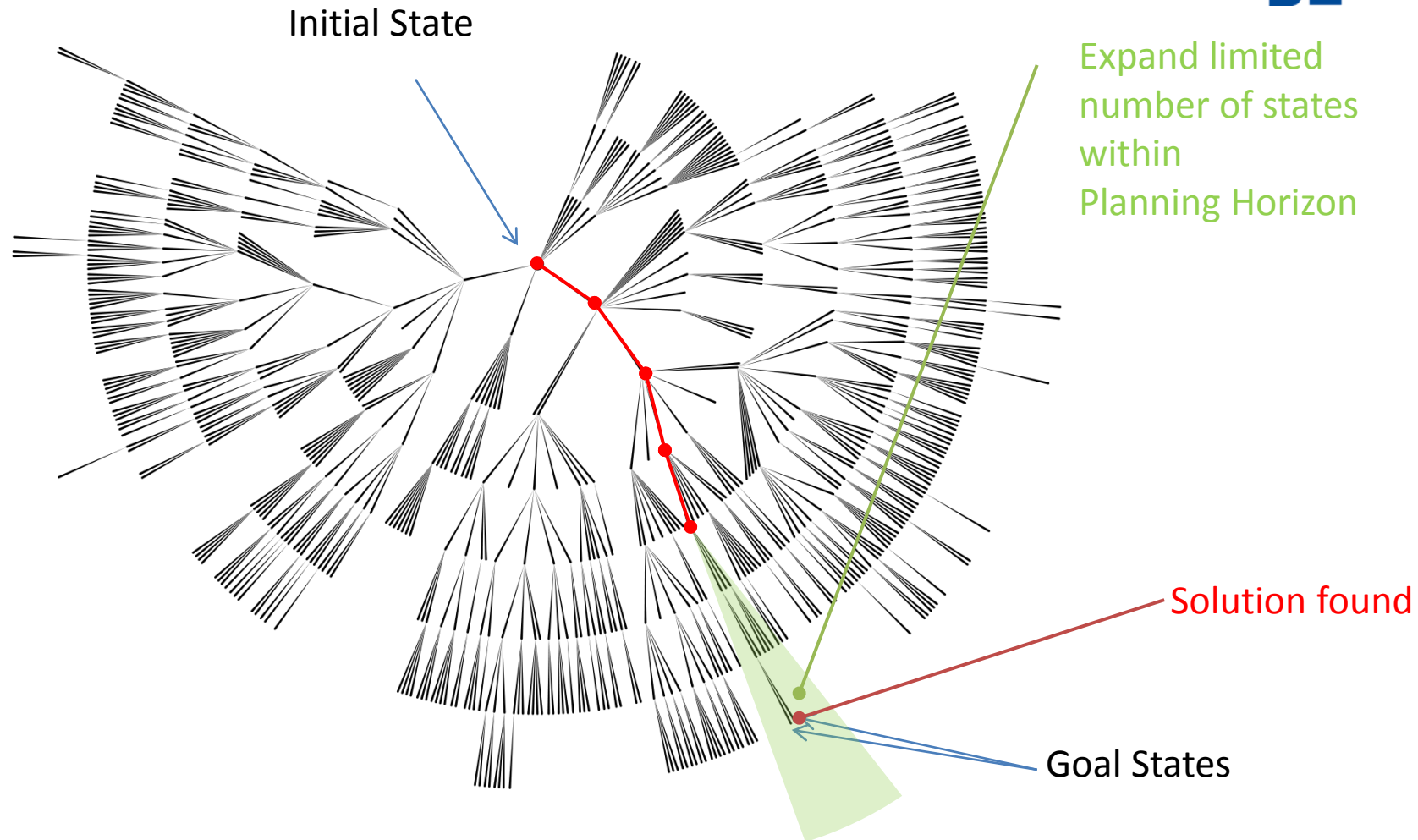
Domain Predictive Control



Domain Predictive Control



Domain Predictive Control





- **Key Aspects**

- Hybrid Systems**

- Continuous Dynamics

- Boolean State Variables

- Autonomy**

- Reduction of Computational Effort

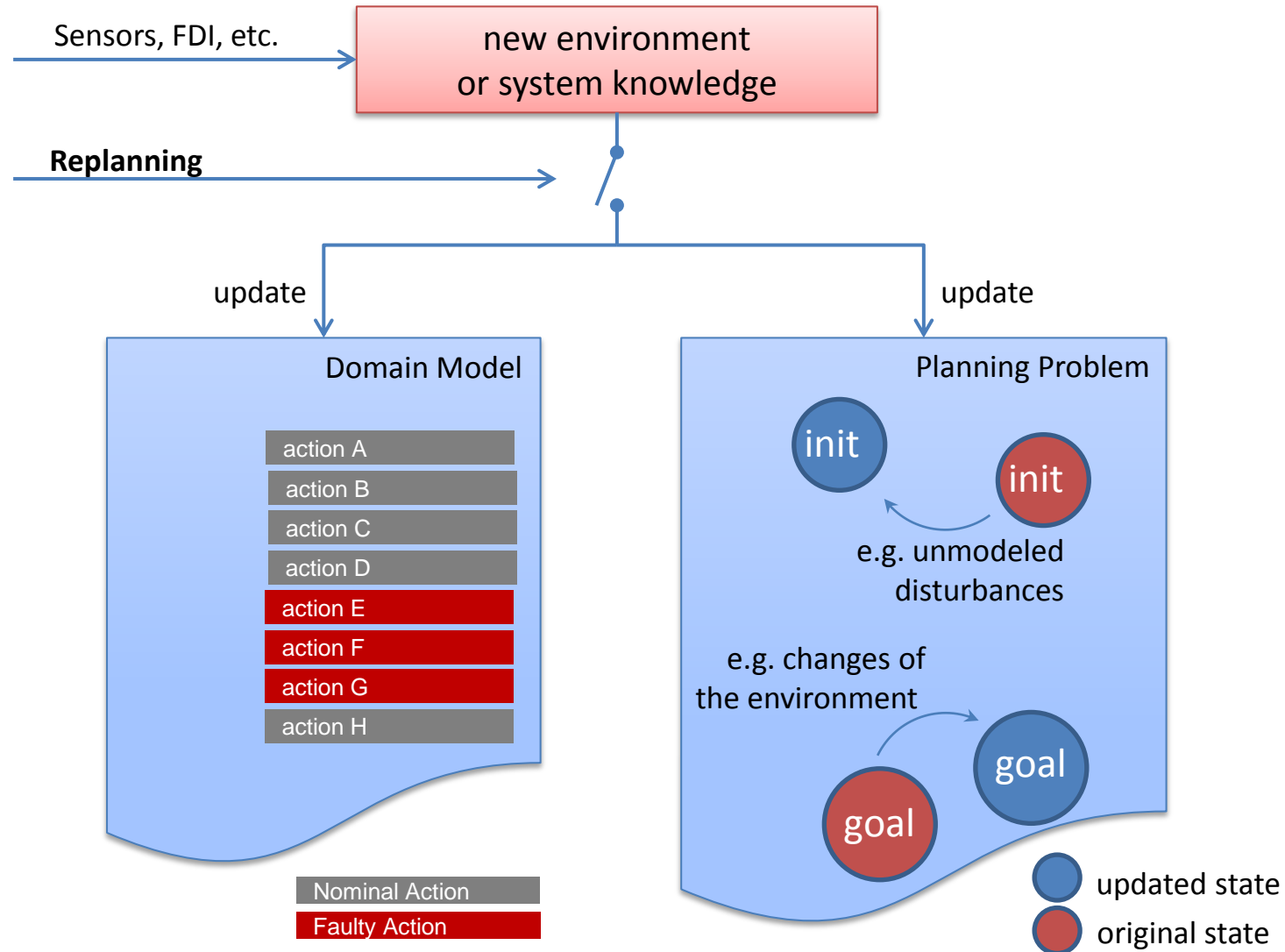
- Quick Decision Generation

- Exogenous Events**

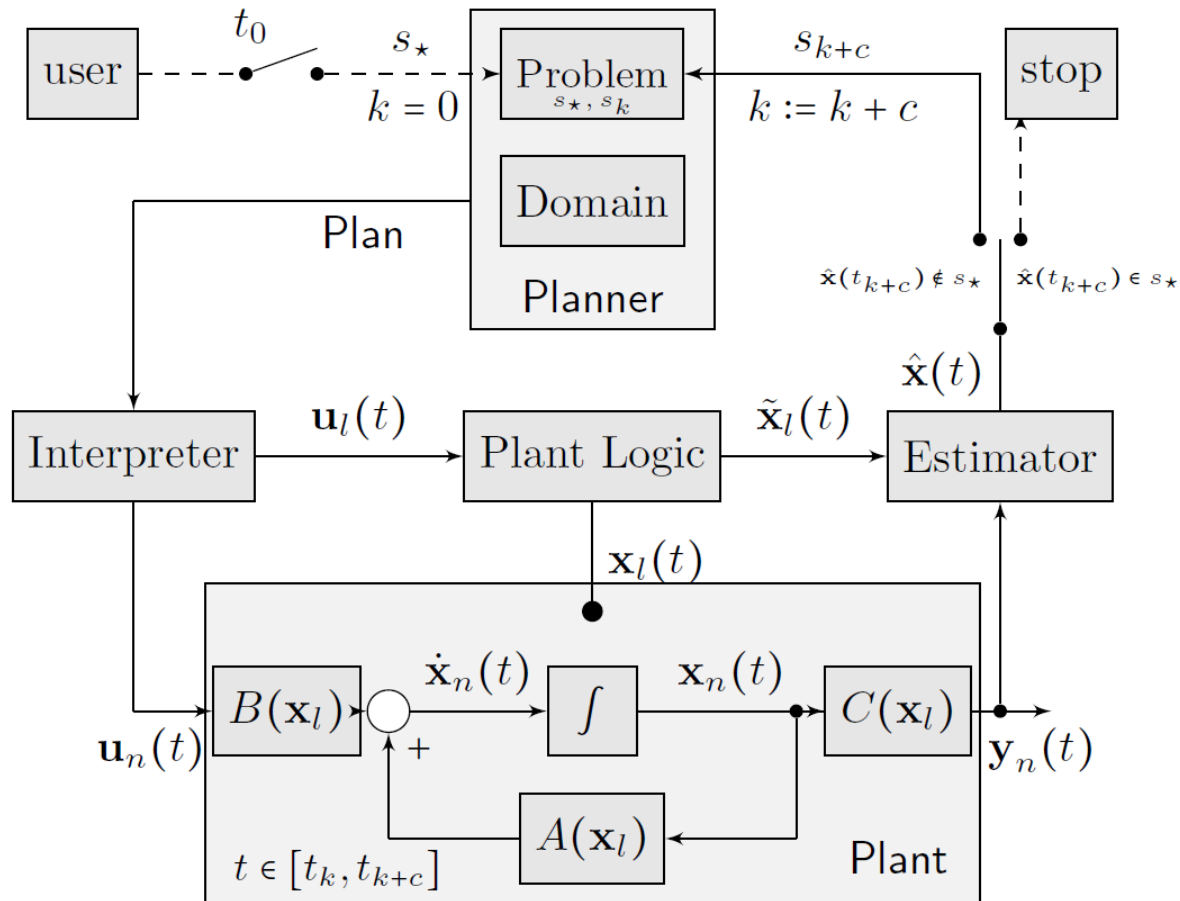
- Obstacles

- Reactivity

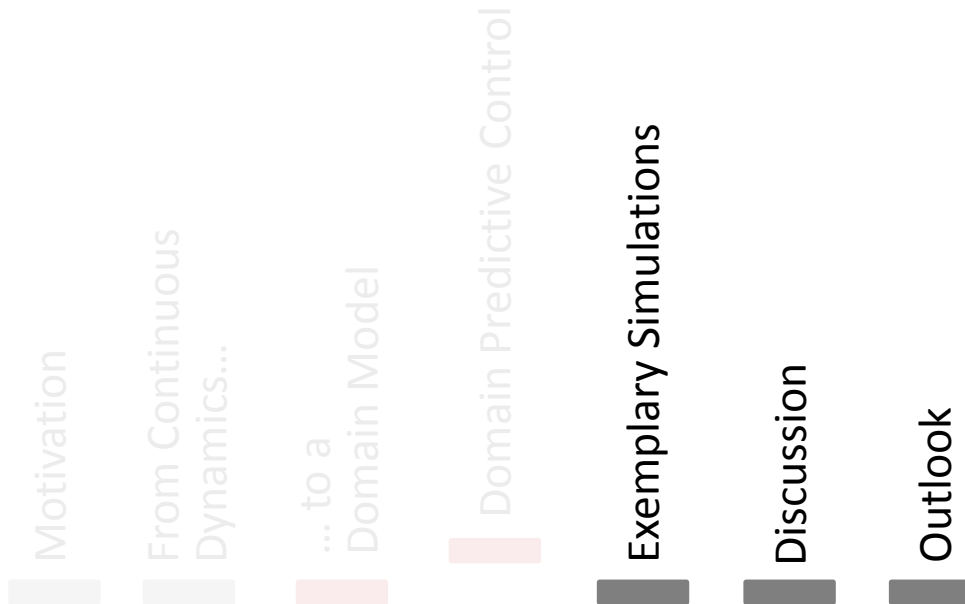
Domain Predictive Control



Domain Predictive Control Arcitecture



Outline



Exemplary Simulation



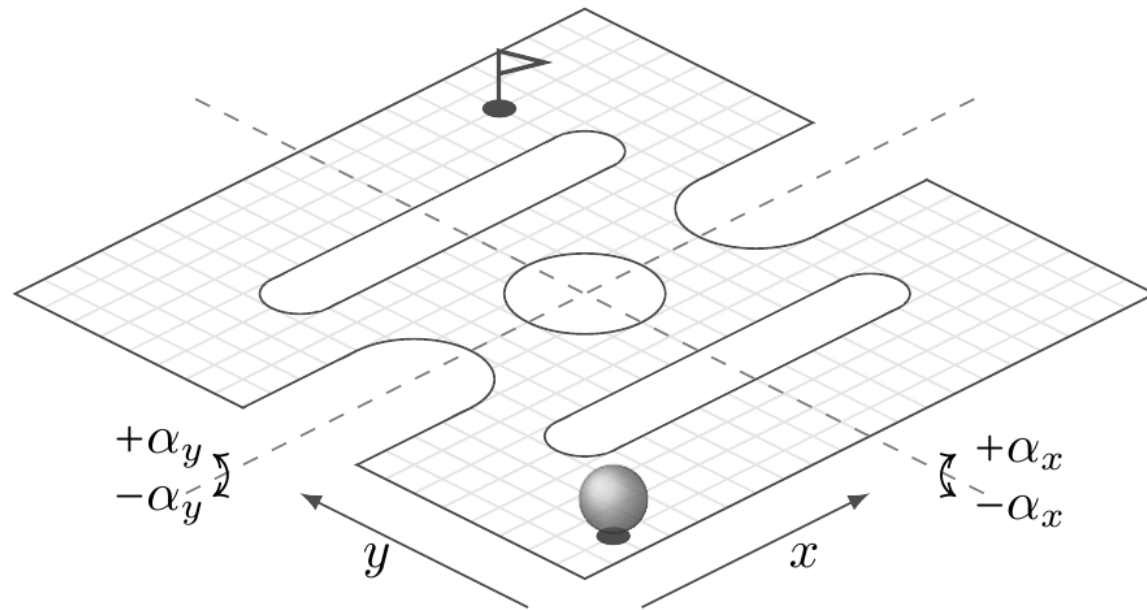
action 0	$\alpha_y = 0^\circ$	$\alpha_x = 0^\circ$
action 1	$\alpha_y = 0^\circ$	$\alpha_x = 2.92^\circ$
action 2	$\alpha_y = 0^\circ$	$\alpha_x = -2.92^\circ$
action 3	$\alpha_y = 2.92^\circ$	$\alpha_x = 0^\circ$
action 4	$\alpha_y = -2.92^\circ$	$\alpha_x = 0^\circ$
action 5	$\alpha_y = 2.92^\circ$	$\alpha_x = -2.92^\circ$
action 6	$\alpha_y = 2.92^\circ$	$\alpha_x = 2.92^\circ$
action 7	$\alpha_y = 2.92^\circ$	$\alpha_x = -2.92^\circ$
action 8	$\alpha_y = -2.92^\circ$	$\alpha_x = -2.92^\circ$



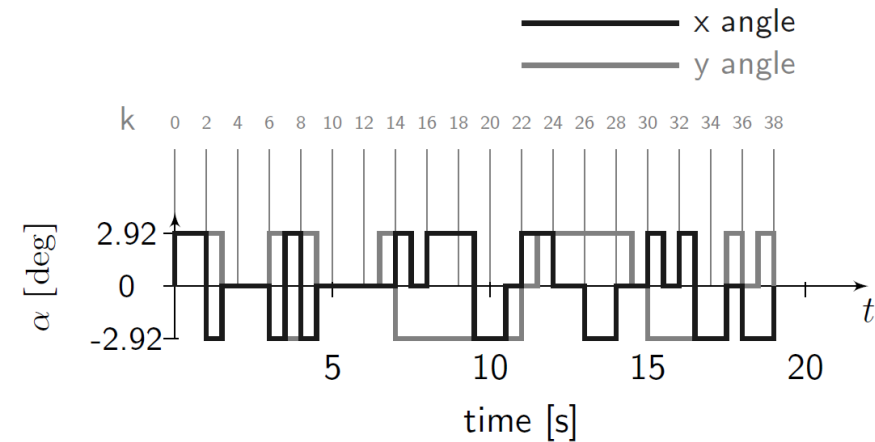
$$\delta_i = 0.5 \text{ s}, \forall i \in [0,8]$$

$p_{\vdash} =$

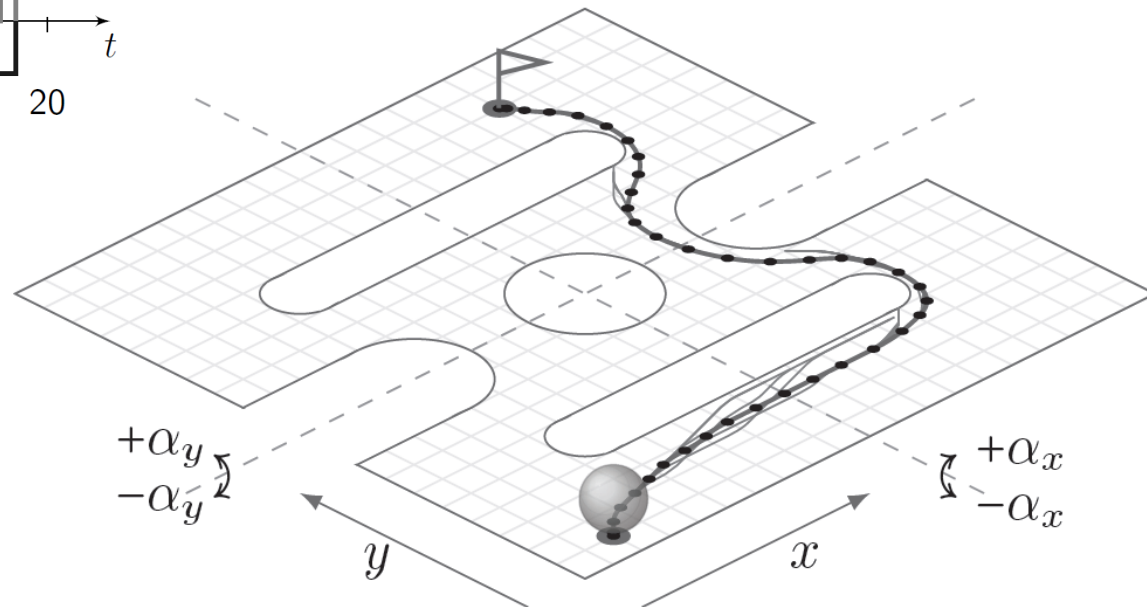
$$\begin{aligned} & [(x > 8) \vee (x < 2) \vee (y > 3) \vee (y < 2)] \wedge \\ & [(x > 6) \vee (x < 4) \vee (y > 6) \vee (y < 4)] \wedge \\ & [(x > 4) \vee (x < 0) \vee (y > 6) \vee (y < 4)] \wedge \\ & [(x > 10) \vee (x < 6) \vee (y > 6) \vee (y < 4)] \wedge \\ & [(x > 8) \vee (x < 2) \vee (y > 8) \vee (y < 7)] \wedge \\ & [(x > 0) \wedge (x < 10) \wedge (y > 0) \wedge (y < 10)] \end{aligned}$$



Exemplary Simulation



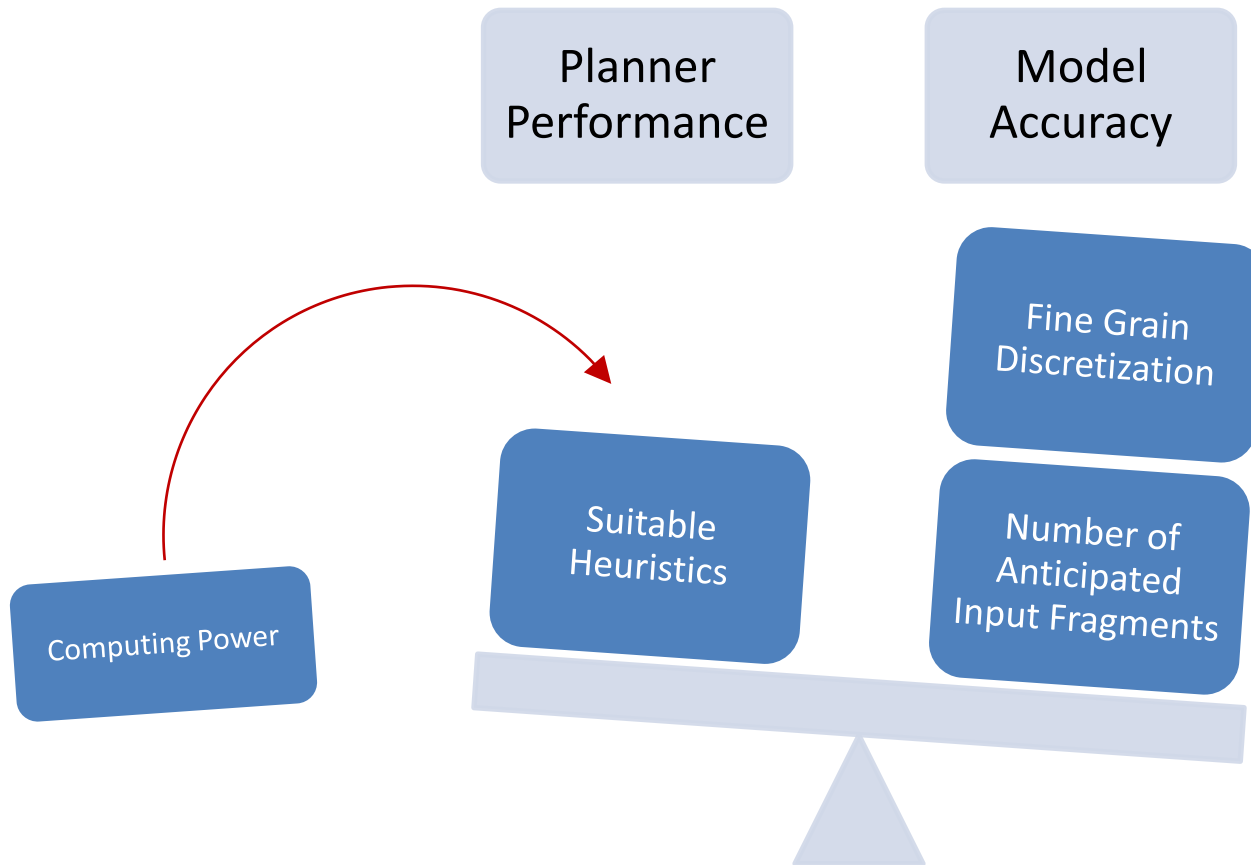
Planned States • • •
 Simulated Trajectory —
 Intermediate Promising Trajectory —



Outline



Discussion



Summary and Conclusion



Pros



- ☐ **general** problem formulation
- ☐ **changing system configurations**
- ☐ restricted state space
- ☐ **failure tolerance**

Cons



- ☐ anticipated input fragments
- ☐ discrete system dynamics
- ☐ computational effort
- ☐ currently: linear systems only

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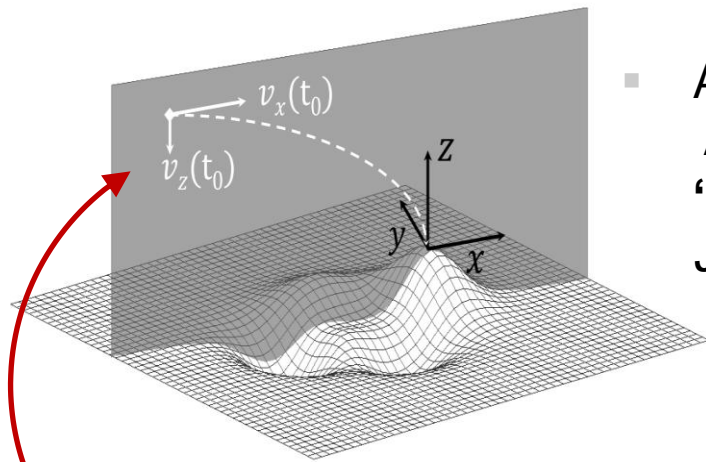
Domain Predictive Control

Exemplary Simulations

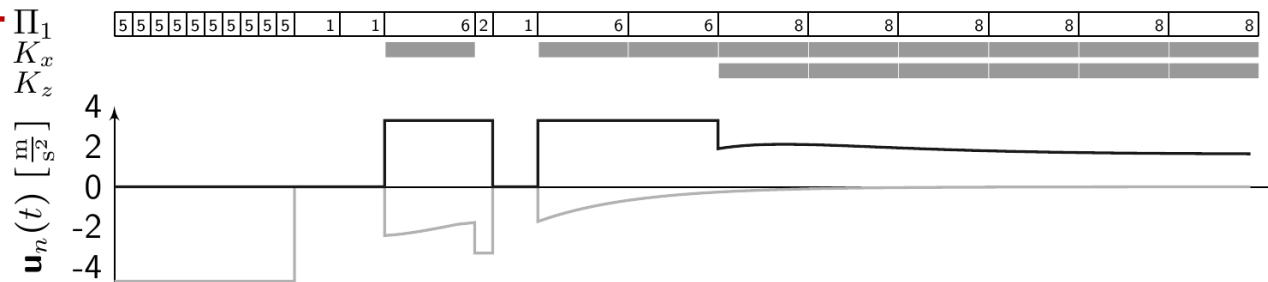
Discussion

Outlook

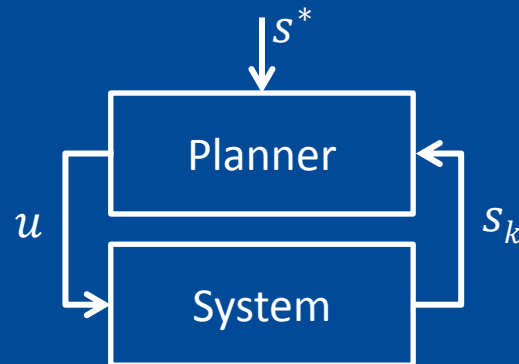
Outlook



- American Institute of Aeronautics and Astronautics
Astrodynamics Specialist Conference (August 2012)
“Planning-based Autonomous Lander Control”
J. Löhr, B. Nebel, and S. Winkler



Planning Based Framework for Controlling Hybrid Systems



Heuristic

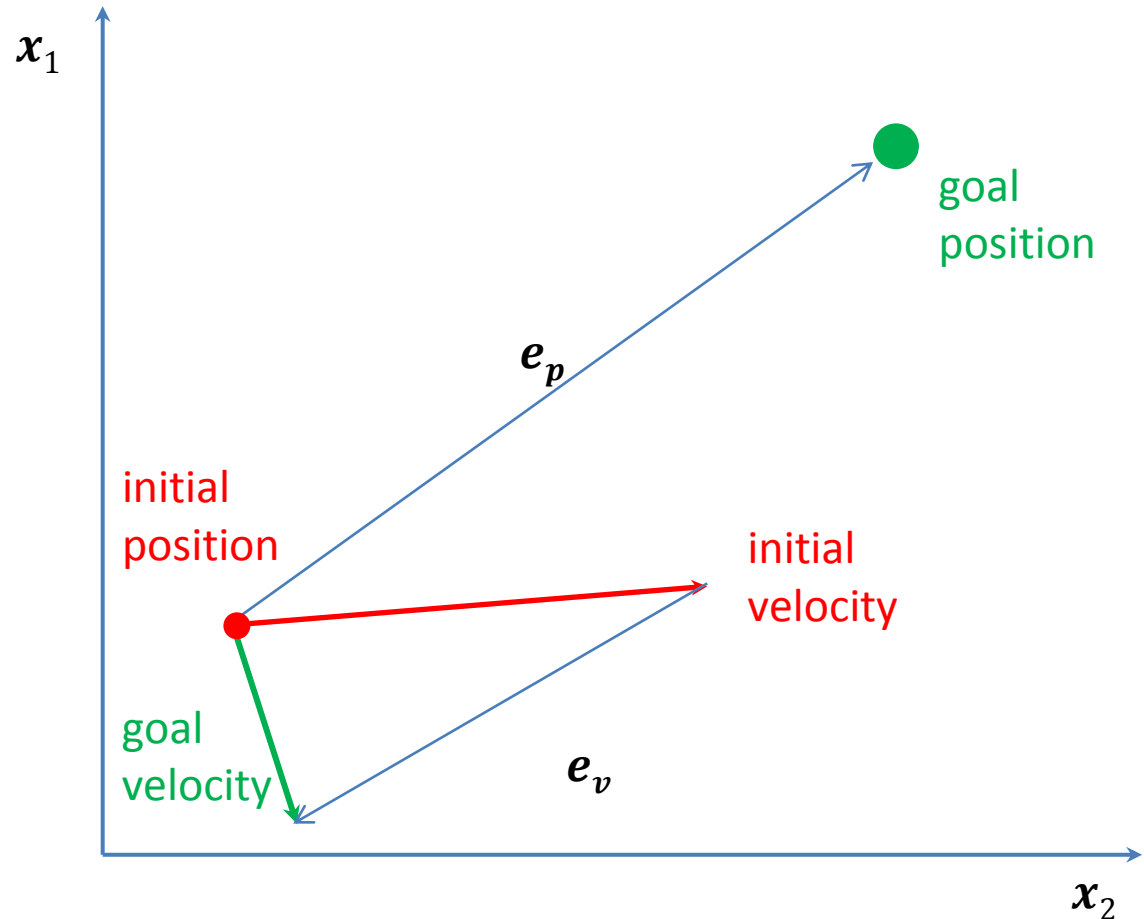


Error State Heuristic

$$h = \|e_p + e_v\|_1$$

Open Heuristic Issues:

1. Weighting of numerical variables
2. Weighting between numerical and logical variables



Stable Dynamics



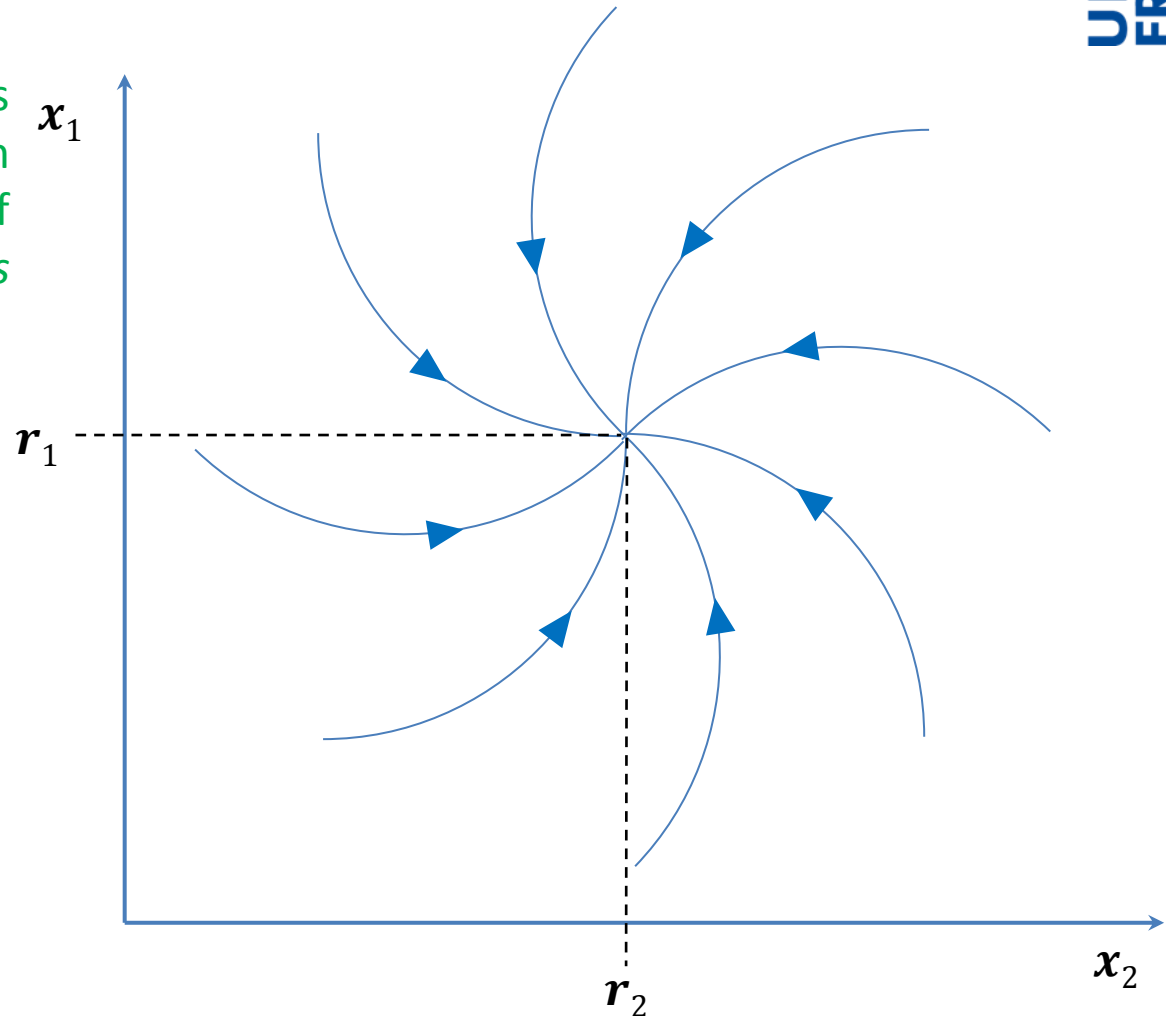
Homogeneous
Solution
of
Stable Dynamics

$$\dot{\mathbf{x}}_n(t) = \mathbf{A}_{cl} \mathbf{x}_n(t) + \mathbf{B} \mathbf{u}_n(t)$$

\mathbf{A}_{cl} state feedback controlled
 $\mathbf{u}_n(t) = -\mathbf{K} \mathbf{x}_n(t)$

closed loop dynamics
 $\mathbf{A}_{cl} = \mathbf{A} - \mathbf{B} \mathbf{K}$

choose controller \mathbf{K} such that
 $\text{Re}(\text{eig}[\mathbf{A} - \mathbf{B} \mathbf{K}]) < 0$



Stable Dynamics



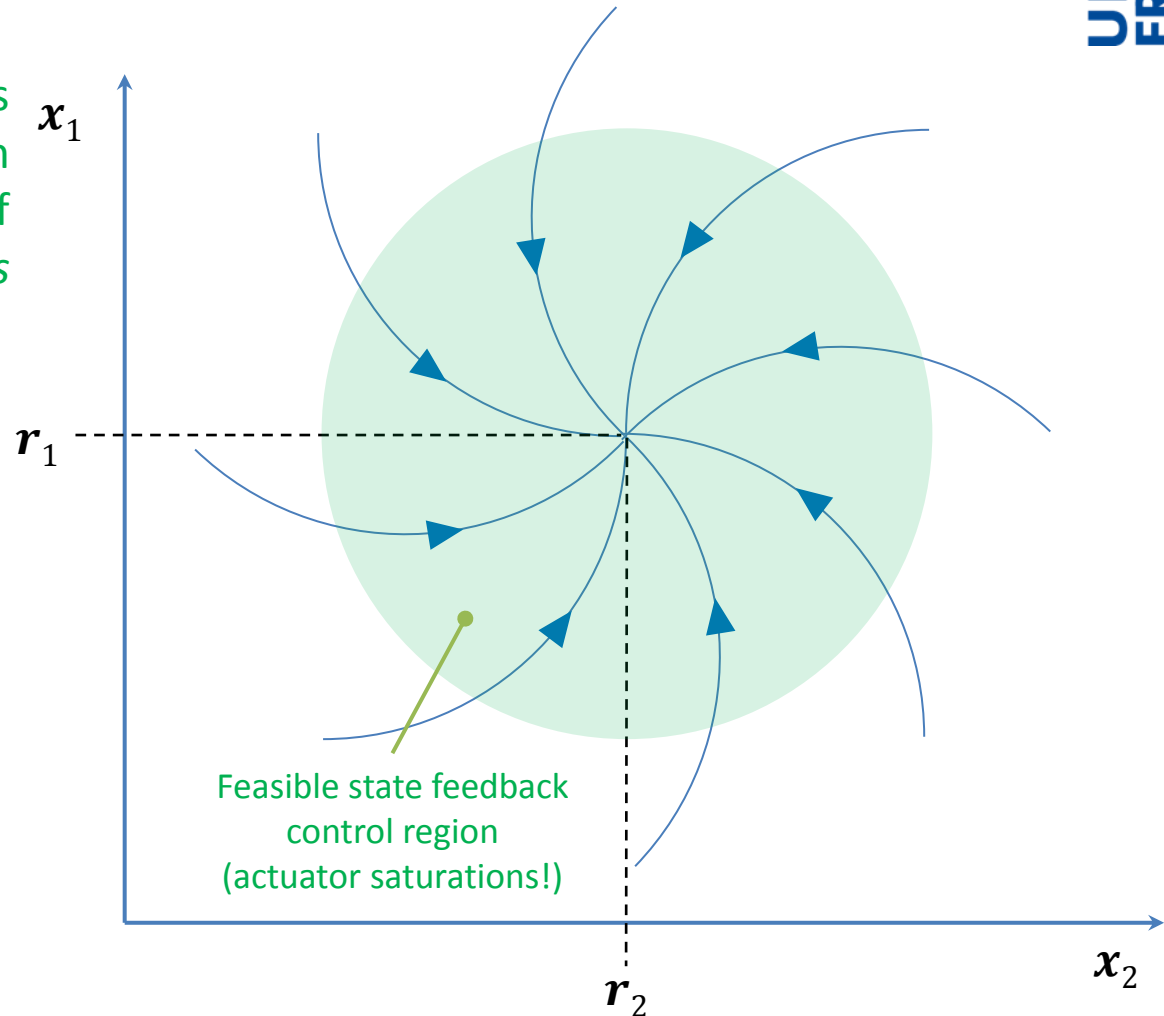
Homogeneous
Solution
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Stable Dynamics

$$\dot{\mathbf{x}}_n(t) = \mathbf{A}_{cl} \mathbf{x}_n(t) + \mathbf{B} \mathbf{u}_n(t)$$

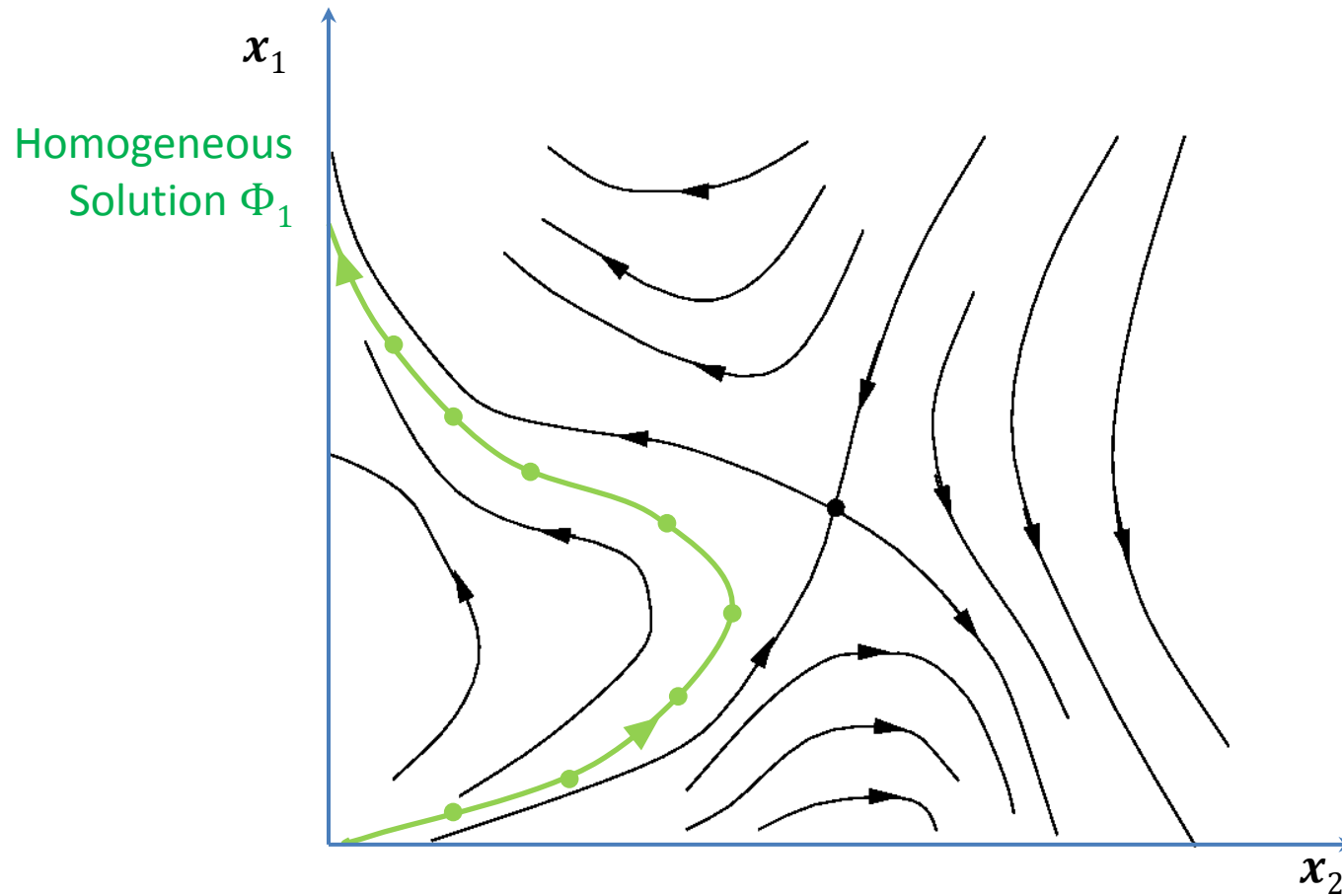
\mathbf{A}_{cl} state feedback controlled
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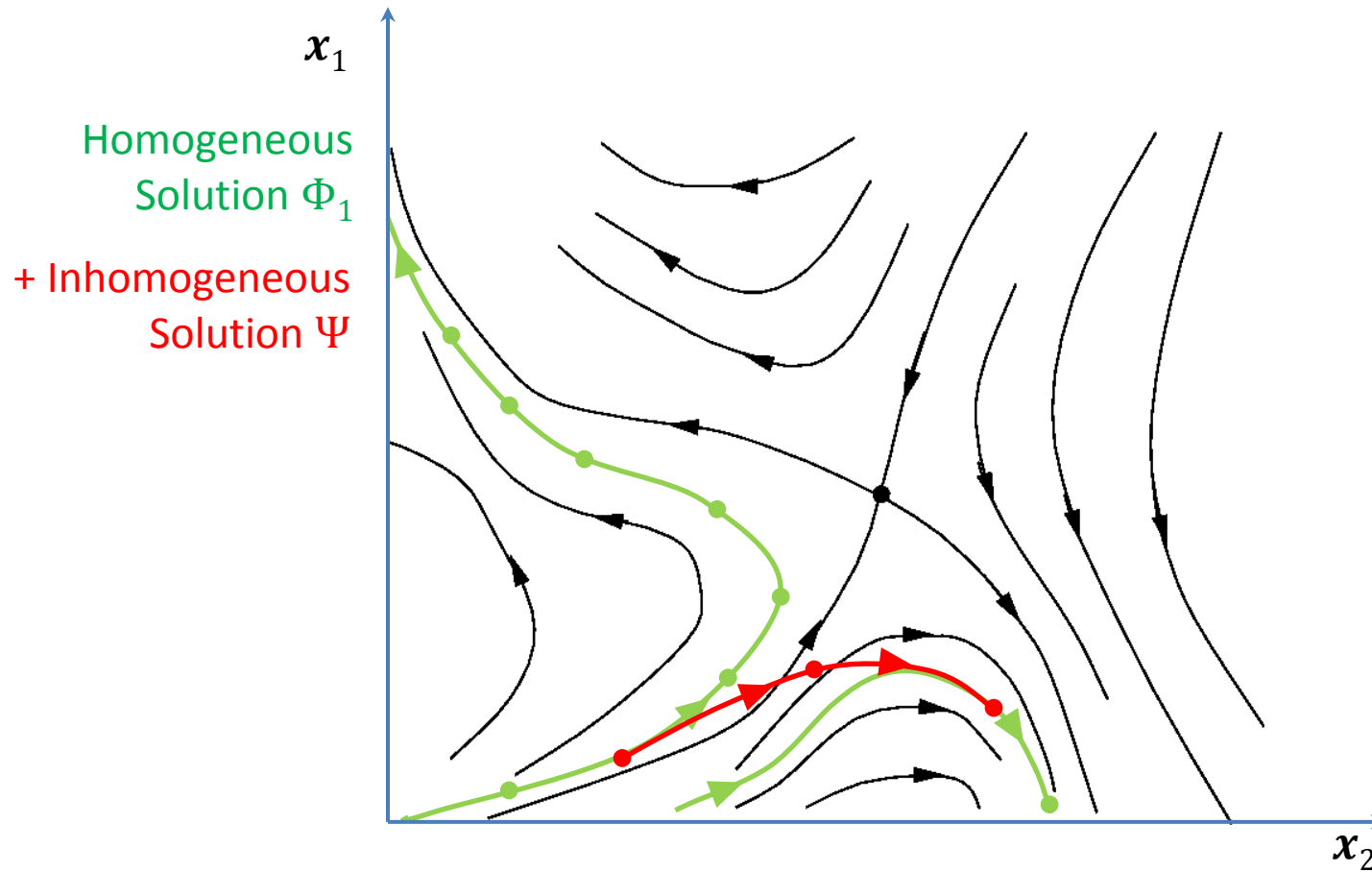
choose controller \mathbf{K} such that
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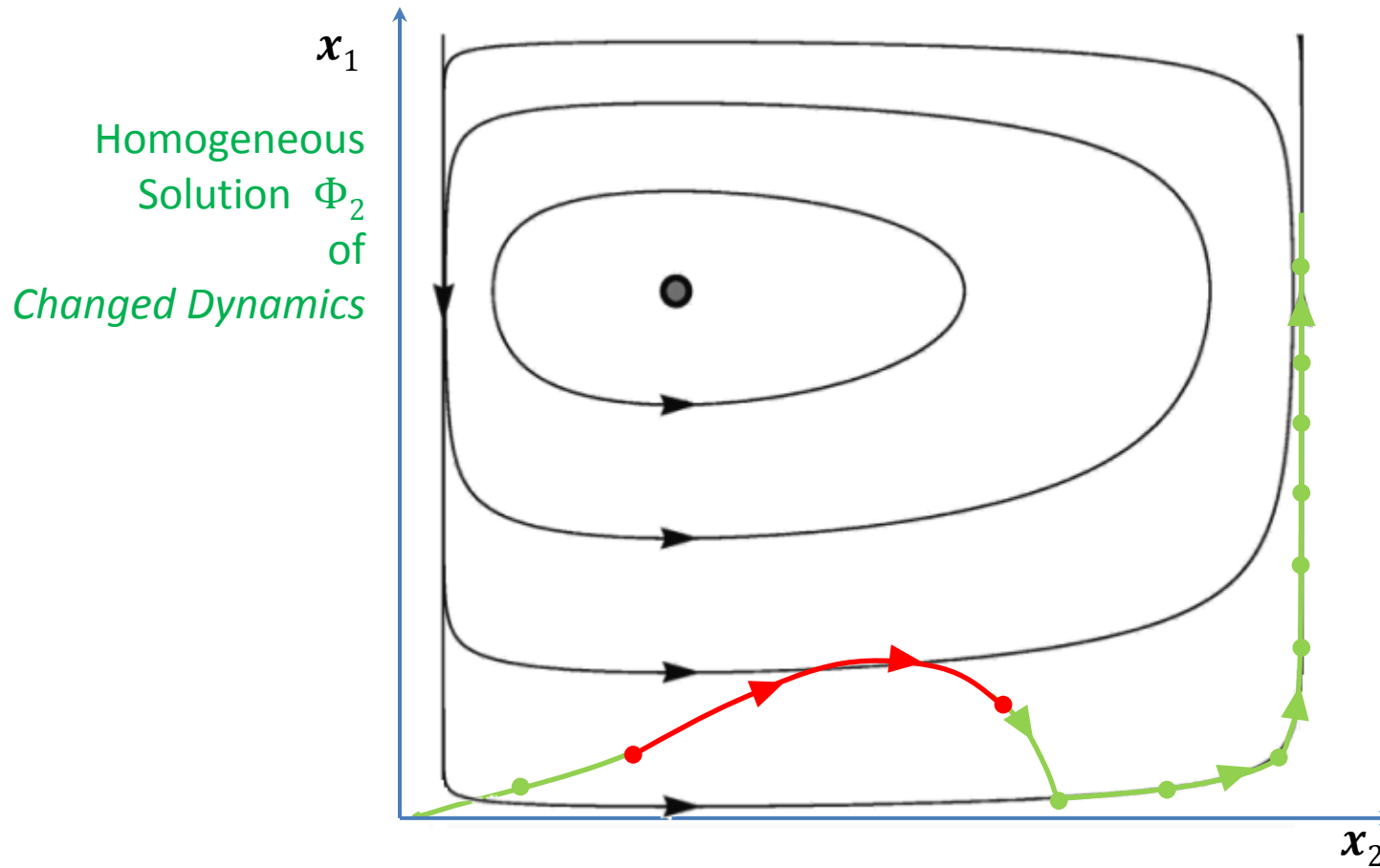
Discretized Dynamics



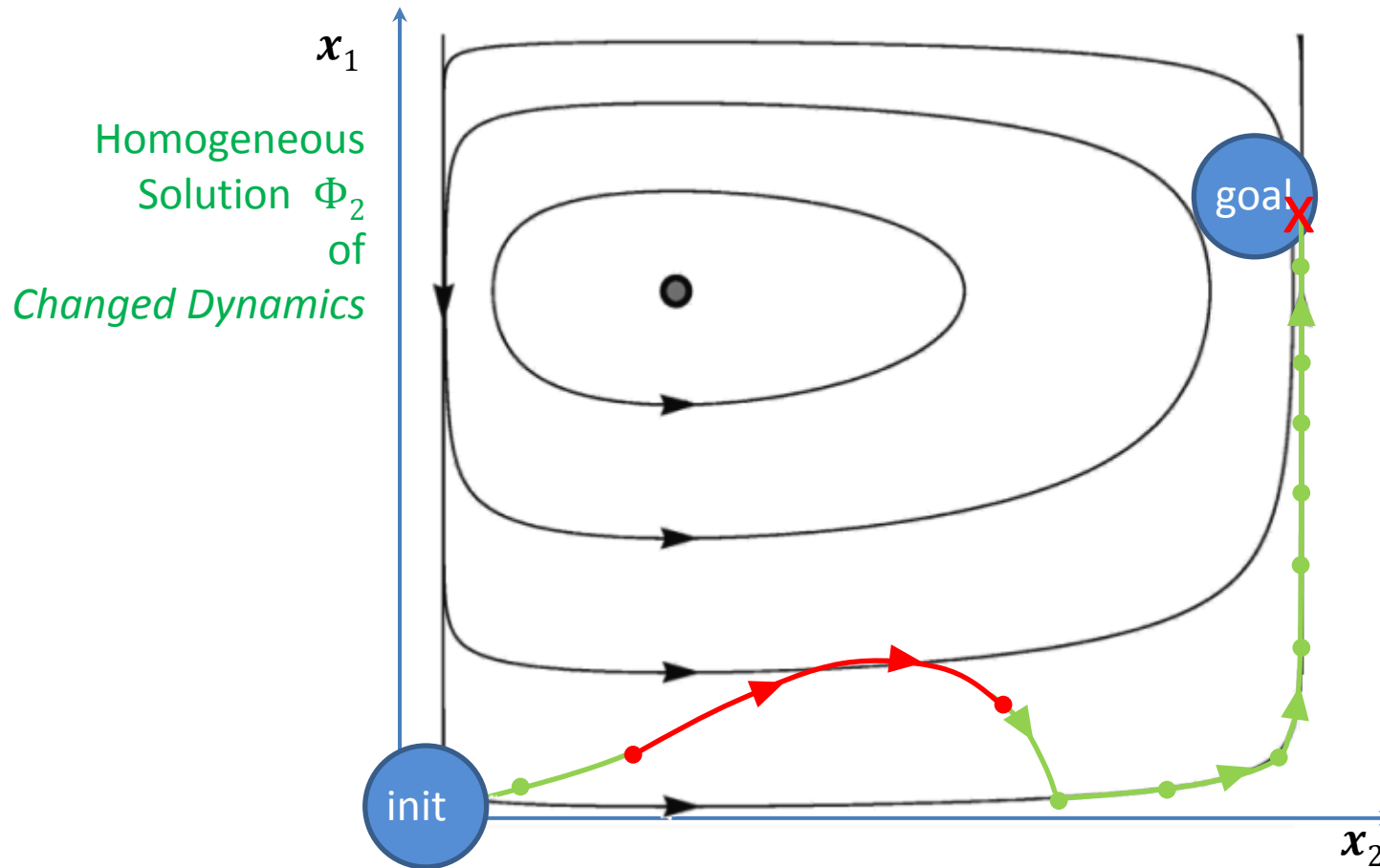
Discretized Dynamics



Discretized Dynamics



Discretized Dynamics



The Domain Model

A Piecewise Affine System?



action A

action B

action C

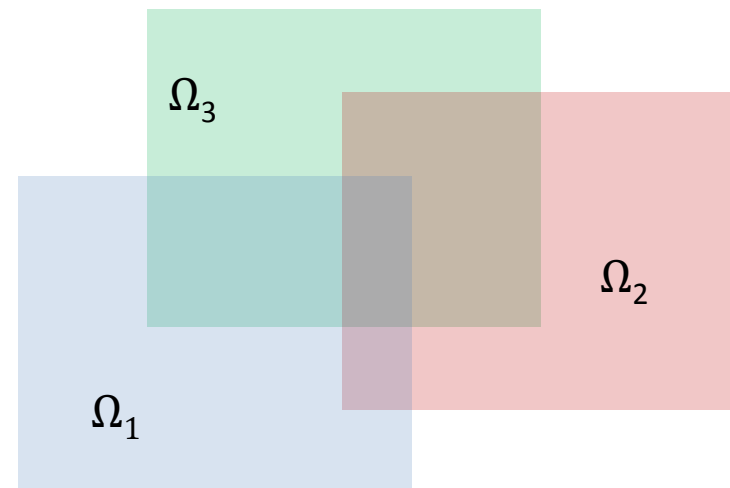
action D

$$\mathbf{x}_n(k+1) = \Phi_i \mathbf{x}_n(k) + \Psi_i, \mathbf{x}_n \in \Omega_i$$

$$\Omega_i \cap \Omega_j = \emptyset, \quad \forall i \neq j$$

$$\Omega_i \cap \Omega_j = \mathcal{X}, \quad \forall i \neq j$$

\mathcal{X} :
is not necessarily empty,
we explicitly allow for overlaps of Ω_i
Depicts the state space we can
choose between actions



Time Discretization

